Negative Concord with Polyadic Quantifiers
The Case of Romanian

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Received: date / Accepted: date

Abstract In this paper we develop a syntax-semantics of negative concord in Romanian within a constraint-based lexicalist framework. We show that n-words in Romanian are best treated as negative quantifiers which may combine by resumption to form polyadic negative quantifiers. Optionality of resumption explains the existence of simple sentential negation readings alongside double negation readings. We solve the well-known problem of defining general semantic composition rules for translations of natural language expressions in a logical language with polyadic quantifiers by integrating our higher-order logical object language in Lexical Resource Semantics (LRS), whose constraint-based composition mechanisms directly support a systematic syntax-semantics for negative concord with polyadic quantification in Head-driven Phrase Structure Grammar (HPSG).

Keywords Negative Concord · Romanian · Polyadic Quantifiers · Head-driven Phrase Structure Grammar · Lexical Resource Semantics

1 Introduction

Negative concord (NC) languages like Romanian pose a formidable challenge to common practices of composing meaning in most current theories of formal semantics. In NC constructions we observe the use of what *prima facie* seem to be several negative expressions in one clause with the overall effect of a single interpreted negation. The negative sentence (1a) with one negative expression (*nobody*) in a non-NC language like standard English thus has the Romanian counterpart in
(1b), a sentence with two negative expressions, the n-word nimeni ‘nobody’ and the obligatory negative marker (NM) nu ‘not’. The co-occurrence of the corresponding expressions nobody and not in (standard) English results in an affirmative interpretation in (1c), which is unavailable in the Romanian sentence (1b).

(1)  
   a. **Nobody** came.  
      \[ \neg \exists x \ [person'(x) \land come'(x)] \]
   b. **Nimeni** *(nu)* a venit.  
      nobody not has come  
      ‘Nobody came.’
      i. \[ \neg \exists x \ [person'(x) \land come'(x)] \]
      ii. \[ \# \neg \exists x \ [person'(x) \land \neg come'(x)] \]
   c. **Nobody** did not come.  
      \[ \neg \exists x \ [person'(x) \land \neg come'(x)] \]
      \[ \equiv \forall x \ [person'(x) \rightarrow come'(x)] \]

The initial assumption that both nimeni and nu have negative semantics is preliminarily confirmed by (2a) and (2b), where each of the two words alone is responsible for the negative interpretation, just like their counterparts in the corresponding English translations.

(2)  
   a. A: Cine a venit?  
      who has come  
      B: Nimeni.  
      nobody  
   b. Ion **nu** a venit.  
      John not has come  
      ‘John didn’t come.’

Two kinds of solutions have been proposed for NC: 1) mechanisms to compose negative meanings by which the apparently gratuitous negations are factored out under certain conditions (Zanutttini (1991), Haegeman (1995), de Swart and Sag (2002), Richter and Sailer (2004)) (“the negative quantifier [NQ] approaches”), and 2) treatments of n-words as negative polarity items, indefinites or existential quantifiers that carry no negative semantics of their own, the negation being contributed by a (possibly, covert) negative operator (Ladusaw (1992), Giannakidou (1998), Zeijlstra (2004), Penka (2011)) (“the negative polarity item [NPI] approaches”). The former analyses argue for a cross-linguistically uniform semantics of n-words on the basis of their negative contribution in contexts like (2). The latter use the obligatoriness of the NM in contexts like (1b) (and, possibly, other language-specific characteristics) to relate the difference between NC languages and non-NC languages to a cross-linguistic variation in the semantics of n-words.

The two principal ways of answering to the NC challenge have their respective characteristic potential shortcomings. Unless it is embedded in a systematic and coherent general theory of semantic composition, negation factorization in NQ approaches easily assumes the air of an ad hoc mechanism and raises serious questions about the nature of the syntax-semantics interface. These techniques tend to be at odds with straightforward renderings of a compositional Montagovian semantics. As for the second school of thinking about NC, a covert negative operator in NPI approaches is hard to take for granted considering the overwhelming
cross-linguistic evidence that n-words overtly contribute negative semantics (see most recently de Swart (2010)). In light of the semantic properties of n-words in Romanian, we will follow the NQ approach and present an analysis of the syntax and semantics of Romanian NC constructions as polyadic quantification in Lexical Resource Semantics (LRS, Richter and Sailer (2004)). Polyadic quantifiers are higher-order functions that receive a mathematically rigorous formulation in Generalized Quantifier Theory (Keenan and Westerståhl (1997), Peters and Westerståhl (2006)) and express relations between more than two sets; the flexible constraint-based composition mechanisms of LRS permit a direct formalization of our theory within HPSG (Pollard and Sag (1994)). The former component of our analysis defeats the ad-hoc character of older NQ approaches, while the latter allows a coherent and systematic syntax-semantics interface for negative concord.

Following a proposal by de Swart and Sag (2002) for French, we express the truth conditions associated with Romanian NC constructions by means of negative polyadic quantifiers. Going beyond de Swart and Sag’s largely informal treatment of the logical representations for polyadic quantification in HPSG, we define a higher-order logic with polyadic quantification and modify the interface principles of LRS to accommodate the newly added quantifiers. This way we arrive at a fully explicit composition theory of Romanian NC using resumptive polyadic quantification. The fact that this is possible at all is of particular interest since resumptive polyadic quantifiers are a notorious problem for frameworks which use the lambda calculus in combination with a functional theory of types to define a syntax-semantics interface for natural languages. Our proposal of implementing them with LRS overcomes these fundamental formal limitations. With a combination of lexical underspecification and constraint-based semantic composition principles, we can express a precise systematic relationship between a surface-oriented syntax and semantic representations with polyadic quantifiers in a constraint-based semantic theory which acknowledges the pre-theoretical intuitive notion that all n-words are semantically negative.

The remainder of the paper is structured as follows: First we discuss the data that lead us to conclude that Romanian n-words are indeed negative quantifiers and multiple n-words in NC configurations form a polyadic quantifier (Section 2). Then we move on to the tools that we need to formulate our theory, and extend the logical object language and the principles of LRS in such a way as to have resumptive polyadic quantifiers at our disposal (Section 3). The core of our theory of Romanian NC is presented in Section 4, where we formulate a language-specific principle that captures the properties of simple Romanian NC constructions. A brief excursion into languages with different NC systems confirms that our theory can be seen as a language-specific instance of a typological theory of NC. In Section 5 we show that our analysis can be extended in a straightforward way to more complex cases which involve scope properties of negative quantifiers in embedded subjunctive clauses. In the final section we briefly summarize the results and speculate about possible future developments.

2 Data

In this section we discuss evidence for the negative semantics of n-words and for their quantificational behavior. Initially we focus on the properties individual n-
words in Romanian and on evidence against their treatment as NPIs. Then we shift our attention to their (polyadic) quantificational properties in NC constructions.

Sentential negation in Romanian is commonly expressed by the verbal prefix *nu* (Barbu (2004)). In the absence of other negative elements, *nu* contributes semantic negation, as in (3a). If in addition an n-word such as *niciun* is present, as in (3b), only a negative concord (NC) reading is available, a double negation (DN) interpretation is not. In constructions with two n-words, both an NC reading and a DN reading are available (see (3c)).

(3) a. Trei studenţi nu au venit.
   ‘Three students didn’t come.’

b. *Niciun* student *(nu) a venit.
   ‘No student came.’ (NC)
   i. ‘No student didn’t come.’ (DN)

   no student NM has come

c. *Niciun* student *(nu) a citit nicio carte.
   ‘No student read any book.’ (NC)
   i. ‘No student read no book.’ (DN)
   no student NM has read no book

The DN reading in (3c) is dependent on a denial context in which speaker A formulates a negative proposition using the n-constituent *nicio carte* and speaker B denies that proposition by means of the n-constituent *niciun student*, as in (4) below.¹ In this context, a NC reading is excluded.²

(4) a. A: Un student *nu* a citit nicio carte.
   ‘Some student didn’t read any book.’
   a student NM has read no book

b. B: *Niciun* student *(nu) a citit nicio carte.
   ‘No student read no book.’
   no student NM has read no book

   (DN/*NC)

d. A: *Niciun* student *(nu) a citit nicio carte.
   ‘No student read no book.’
   no student NM has read no book

As (3b) indicates, the negative marker (NM) *nu* is always obligatory in finite sentences with n-words. Romanian thus qualifies as a strict negative concord language according to Giannakidou (2007), unlike most of the other Romance languages, which are non-strict NC, as illustrated by the Italian example in(5), where a preverbal n-word occurs without a negative marker. It is only outside the domain of finite verb constructions that Romanian displays what at first seems like a similar behavior: A preverbal n-word is the single exponent of negation with a past participle in (6). In Section 4.3 we will see that this is not a characteristic

¹ See also Fǎlǎuş (2007) and de Swart (2010), for further DN examples in Romanian and other strict NC languages, and Iordǎchioaia (2010), for details on the information structure of DN sentences in Romanian.

² An NLLT reviewer correctly points out that if the denial of speaker B targets the object position of speaker A’s utterance (e.g., A: No student read *this book*; B: No student read *no book*), the DN reading is not available anymore in Romanian. This is most likely due to the the different information structural status of subjects and objects in Romanian, an issue that needs further investigation independently of negation.
property of Romanian NC with non-finite verbs but rather due to the adjectival nature of the participle in this particular construction.

(5) \textbf{Nessuno} é venuto.
Nobody is come
‘Nobody came.’

(6) articol \textbf{de nimeni} citat
article by nobody cited
‘article which hasn’t been cited by anybody’

To solve the problem that NC poses, NPI approaches postulate that n-words like the ones in (3b) and (3c) are in fact negative polarity items without inherent semantic negation (Ladusaw (1992)). Such theories, however, cannot account for the DN reading in (3c). The data set in (3) suggests that (a) the negative marker \textit{nu} contributes negation in the absence of n-words (3a), (b) the negative marker does not contribute negation in the presence of n-words (see the NC reading in (3b), (3c)), and (c) n-words are exponents of semantic negation (see the DN reading in (3c)). As one of its main features, our syntax-semantics interface for Romanian NC acknowledges the lexically negative semantics of n-words and of the NM, and it captures under what circumstances the inherent negativity of the NM can be observed.

2.1 Negative semantics for n-words

Besides the DN reading in (3c), evidence for the inherent negativity of n-words comes from fragmentary answers such as (7) and the past participial constructions illustrated in (6), where in the absence of a verb that would normally carry the NM, n-words contribute negation alone.

(7) A: Cine era la ușă? B: \textbf{Nimeni.} / *Era \textbf{nimeni}.
who was at door nobody/ was nobody
‘A: Who was at the door? B: Nobody.’

In addition, a fragmentary answer to a negative question triggers DN in (8). This makes the ellipsis explanation of NPI approaches (as in Giannakidou (2007)) invalid for (7). If the NM \textit{nu} is elided, it triggers DN in a fragmentary answer with an n-word as in (8). By contrast, what is elided in (7) must be a semantically positive segment (see also Watanabe (2004)). Note that neither one of the putative elided structures would form a grammatical overt structure in Romanian, either because it would be syntactically ill-formed (7) or because it would receive a reading incompatible with the question (8).

(8) A: Ce \textbf{nu} ai citit? B: \textbf{Nimic.} / #\textbf{Nu} am citit \textbf{nimic}.
what NM have read nothing/NM have read nothing
‘A: What didn’t you read? B: Nothing (= I read everything)./ #I read nothing.’
Even more, we can show that in these contexts n-words exhibit anti-additivity (9), and they can consequently license NPIs in their scope:\(^3\) The NPI \textit{vreo} is licensed by the anti-additive n-word \textit{nimeni} but not by the universal quantifier \textit{toat\’a} in the same position (10).\(^4\)

(9) a. A: Who was at the door?
   B: \textbf{Nimeni cunoscut sau important.} = \textbf{Nimeni cunoscut \textit{\&} nimeni important.}
   nobody known or important nobody known and
   nobody important

   b. articol \textit{[de nimeni citat sau l\’audat]} = articol \textit{[de nimeni citat \& de nimeni l\’audat]}
   article by nobody cited or praised article by nobody cited and by nobody praised
   ‘article which hasn’t been cited or praised by anybody’

(10) articol \textit{[de nimeni/*de toat\’a lumea citat la vreo conferin\’\c{t}a]}
   article by nobody/by all people cited at any conference
   ‘article which hasn’t been cited by anybody at any conference’

2.2 No semantic licenser for n-words

NPI approaches to NC rest on two claims: (a) n-words lack negation, and (b) they are semantically licensed by an anti-additive operator. This operator assumes the central role of contributing the single negation to the utterance. Ladusaw (1992) argues that the semantic licenser of NPIs may be covert. This proposal has been widely exploited in the Minimalist tradition (see, for instance, Zeijlstra (2004)). Like many proponents of surface-oriented syntactic frameworks, we find it conceptually highly dubious to ascribe an essential aspect of the semantics of an entire class of utterances to invisible objects whose presence is intrinsically almost impossible to falsify. Rejecting the option of postulating an empty syntactic operator, the only remaining plausible licenser of n-words in a NC construction like (3b) is the NM. In Romanian the NM is usually obligatory with n-words, which has been interpreted as a consequence of its function as a semantic licenser. Analyses that adopt this view were formulated for Polish in Przepiórkowski and Kupšć (1999) and Richter and Sailer (1999), and for Romanian in Ionescu (1999) (see also Isac (2004) for a generative NPI approach). We do not think that this idea is correct and show instead that although the Romanian NM is obligatory with n-words, it does not behave like a \textit{semantic} licenser, mainly because n-words, as carriers of negation, do not need one. Evidence for this view is brought from the lack of anti-additivity of the NM in combination with n-words, and from the syntactic independence of n-words from the NM.

\(^3\) A function \(f\) is anti-additive iff for each pair of sets \(X\) and \(Y\), \(f(X \cup Y) = f(X) \cap f(Y)\).

\(^4\) Although \textit{vreun/vreo} behave as NPIs with negation, their distribution is more complex than this might suggest. See Farkas (2002) for more details and Fălăuș (2010) for a recent discussion of the distribution of \textit{vreun} outside negative contexts.
First, according to Ladusaw, the semantic licenser of n-words must be at least anti-additive. In the absence of n-constituents, the NM nu receives an anti-additive interpretation as in (11).

(11) a. Studenții nu au citit romane sau poezii.
    students-the NM have read novels or poems
    ‘The students haven’t read novels or poems.’

b. = Studenții nu au citit romane și studenții nu
    students-the NM have read novels and students-the NM
    have read poems
    = ‘The students haven’t read novels and the students haven’t
    read poems.’

If the disjunction that nu takes as argument contains n-words, anti-additivity disappears, and the two n-words are interpreted independently under the scope of negation as in (12). The only reading that survives is one that presupposes ellipsis, which is also available in (11) (but is not relevant for our discussion).

(12) a. Studenții nu au citit niciun roman sau nicio poezie.
    students-the NM have read no novel or no poem
    ‘The students read no novel or no poem.’

b. ≠ Studenții nu au citit niciun roman și studenții
    students-the NM have read no novel and students-the
    nu au citit nicio poezie.
    NM have read no poem
    ≠ ‘The students read no novel and the students read no poem.’

c. = Studenții nu au citit niciun roman sau studenții
    students-the NM have read no novel or students-the
    nu au citit nicio poezie.
    NM have read no poem
    = ‘The students read no novel or the students read no poem.’

If the n-words in (12) are replaced with weak or strong NPIs, the anti-additivity test succeeds. The contrast between (12), on the one hand, and (13)–(14), on the other, shows that nu acts as a semantic licenser for NPIs, but not for n-words.5

(13) a. Studenții nu au citit vreun roman sau vreo poezie.
    students-the NM have read any novel or any poem
    ‘The students didn’t read any novel or any poem.’

b. = Studenții nu au citit vreun roman și studenții
    students-the NM have read any novel and students-the
    nu au citit vreo poezie.
    NM have read any poem
    = ‘The students didn’t read any novel and the students didn’t
    read any poem.’

5 We thank an anonymous NLLT reviewer for bringing the strong NPI data in (14) to our attention.
Second, it is a well-known fact since at least Ladusaw (1980) that the semantic licensing of NPIs usually also presupposes syntactic licensing: semantic licensing can only take place if the NPI is in the syntactic scope of its negative licenser. This condition holds even for the weakest forms of NPIs like *any in English and *vreun in Romanian. They are licensed at long distance, but cannot precede their licenser:

\[ \text{(14) a. } \text{Ion } \text{nu a scos o vorbă sau închis un ochi de la accident.} \]
\[ \text{John has pulled out a word or closed an eye since accident.} \]
\[ \text{‘John hasn’t said a word or slept a wink since the accident.’} \]

\[ \text{(14) b. } \text{= Ion } \text{nu a scos o vorbă şi nu a închis un ochi de la accident.} \]
\[ \text{John NM has pulled out a word and NM has closed an eye since accident} \]
\[ \text{= ‘John hasn’t said a word and hasn’t slept a wink since the accident.’} \]

Moreover, the stronger the licenser the closer it tends to be to the licenser. NPIs like Romanian prea ‘too’ or English *a bit, really* must be in the same clause as their licenser (see also van der Wouden (1997) for English and Dutch):

\[ \text{(15) a. } \text{Ion } \text{nu a zis că a citit vreun roman.} \]
\[ \text{John NM has said that he read any novel} \]
\[ \text{‘John didn’t say that he read any novel.’} \]

\[ \text{(15) b. *vreun student } \text{nu a citit romanul.} \]
\[ \text{any student NM has read novel-the} \]
\[ \text{‘Any student didn’t read the novel.’} \]

If n-words were to be semantically licensed by the NM, they would obviously violate the syntactic condition of semantic licensing as they may precede the NM (see (1b), (3b), (3c)), unlike any other kind of licensees of negation.

In the next section we will see that the locality conditions for the (syntactic) licensing of n-words by the NM are identical to the scope locality conditions of bona fide quantifiers. This will provide evidence that n-words behave like true quantifiers, supporting the view that they are indeed negative quantifiers.

2.3 Locality conditions on n-words

Besides their inherent negative semantics and their lack of semantic licensers, n-words display scope properties that are similar to those of universal quantifiers.
and contrast with the locality conditions of NPI licensing, as first observed in Giannakidou (1998) for Greek. We observe that n-words can enter NC with a NM across a subjunctive clause boundary (17a), but not across a ‘that’ complementizer, which is a constellation in which an NPI can be licensed (17b). This behavior finds its counterpart in universal quantifiers, which can take wide scope over an operator in the matrix clause from an embedded subjunctive clause (18a), but not from an embedded ‘that’-clause (18b).

(17) a. Ion nu a încercat să citească nicio carte.
   John NM has tried SJ read no book
   ‘John didn’t try to read any book.’
   b. Ion nu a zis că a citit vreo/*nicio carte.
      John NM has said that has read any/no book

(18) a. Un student a încercat să citească fiecare carte.
   a student has tried SJ read every book
   ‘Some student tried to read every book.’
   i. $\exists > \forall$;   ii. $\forall > \exists$
   b. Un student a zis că a citit fiecare carte.
      a student has said that has read every book
      ‘Some student said that s/he read every book.’
      i. $\exists > \forall$;   ii. $\# \forall > \exists$

In addition, adjunct clauses and relative clauses block NC formation (19) and wide scope of embedded universal quantifiers (20), but not NPI licensing (19):

(19) a. Nu am dezvăluit secrete [care să-l fi expus pe NM have revealed secrets that SJ-CL be exposed PE
   *niciun/vreo coleg],
      no/any colleague
   ‘I didn’t reveal secrets that exposed any colleague.’
   b. Nu am spus asta [pentru că mi-o ceruse *niciun/vreo
      NM have said this because CL-CL asked no/any
      prieten].
      friend
   ‘I didn’t say that because any friend had asked me to.’

(20) a. Un student a dezvăluit secrete [care l-au expus pe a student has revealed secrets that CL-CL asked PE
   fiecare coleg],
      every colleague
   ‘Some student revealed secrets that exposed every colleague.’
   i. $\exists > \forall$;   ii. $\# \forall > \exists$
   b. Un student a spus asta [pentru că i-o ceruse fiecare
      a student has said this because CL-CL asked every
      prieten].
      friend
   ‘Some student said that because every friend had asked him to.’
   i. $\exists > \forall$;   ii. $\# \forall > \exists$
Isac (2004) argues against the quantificational status of Romanian n-words. In a syntactic analysis she claims that only preverbal n-words are quantificational (due to their assumed focus position), while the postverbal ones are non-quantificational. This is intended to be shown by the ability of the preverbal n-word to take wide scope over the quantifier *mai mult de doi* ‘more than two’ in (21a), and the inability of the postverbal n-word to take wide scope over the quantifier *cel puțin doi* ‘at least two’ in (21b). Isac assumes that (21b) only has one interpretation, but remains silent about whether a wide scope reading for *mai mult de doi* is available in (21a).

(21) a. Niciun copil n-a văzut *mai mult de doi hoți.*  
no child NM-has seen more than two thieves  
NO > MORE THAN TWO: ‘No child saw more than two thieves.’

b. *Cel puțin doi* copii n-au văzut niciun hoț.  
at least two children NM-have seen no thief  
AT LEAST TWO > NO: ‘At least two children saw no thief.’

Quantifier scope in Romanian is determined by an interplay between linear order and the c-command relations between the quantifiers (see Iordăchioaia (2010, Section 3.5), for details). On that basis the scope preference in (21) is expected, given that *niciun copil* and *cel puțin doi copii* are in the subject position and also precede *mai mult de doi hoți* and *niciun hoț*, respectively.

According to Isac’s line of reasoning, *mai mult de doi* is a true quantifier. Under the right contextual conditions it should thus take wide scope over the preverbal subject n-word from its object position. According to our native speaker informants, a wide scope reading is slightly easier to obtain for *mai mult de doi* in (21a) than for the postverbal n-word *niciun* in (21b). But this preference does not prove that the n-word in postverbal position is less quantificational than a non-negative quantifier as Isac’s analysis predicts. The same scope preference can be observed in English, a DN language where it is standardly assumed, even in Isac (2004), that n-words are always negative quantifiers:

(22) a. *No* child saw *more than two* thieves.  
i. NO > MORE THAN TWO  
ii. ? MORE THAN TWO > NO

b. *At least two* children saw *no* thief.  
i. AT LEAST TWO > NO  
ii. ?? NO > AT LEAST TWO

More corroborating evidence for the quantificational nature of Romanian n-words comes from the scope blocking effect of English ‘that’-clauses and the lack of this effect in ‘to’-infinitives. While a wide scope reading of the embedded negative quantifier is impossible in (23b), it is available in (23a). Considering that the infinitival construction corresponds to a subjunctive clause in Romanian, the scope properties of Romanian n-words, illustrated in (17), are similar to those we observe here for negative quantifiers in English.

(23) a. John tried to read *no* book.  
i. John tried not to read any book.  
ii. John didn’t try to read any book.
b. John said that he read no book.
   i. John said that he didn’t read any book.
   ii. # John didn’t say that he read any book.

We conclude that n-words in Romanian are negative quantifiers. Following Ionescu (1999, 2004), we take their dependence on the presence of a NM to indicate that their sentential scope must be marked on the main verb. This is a purely syntactic licensing condition, unlike the semantic licensing of NPIs in the scope of an appropriate semantic operator. A detailed discussion of embedded subjunctive clauses with NC in Section 5.1 will provide further support for this analysis. Unlike the proposal that we develop here, Ionescu (1999, 2004) argues that n-words are existential, not negative quantifiers. Under the existential quantifier hypothesis, however, it is unclear why the scope properties of n-words illustrated in (17a) should differ from those of existential NPIs (typical existential quantifiers whose scope is marked by sentential negation) exemplified in (17b). It is equally unclear how one would derive the DN reading in (3c).

Syntactic licensing of negative quantifiers by a scope marker might be considered an odd phenomenon by some. But note that negative quantifiers are the only quantifiers for which there is a truth-conditionally equivalent operator that appears on the verb. It might then be not entirely unexpected that a language enlists the available operator to disambiguate difficult scope facts in complex sentences by apparent syntactic-semantic redundancy.\(^6\) We speculate that the potential perceptive advantage of such a strategy might even be one of the factors that drive a grammatical system with an independent negative interpretation of negative markers on the verb toward an NC system of the type that Romanian represents.

The negative semantics and the quantificational properties of n-words that we have argued for explain the possibility of a DN reading with two n-words: it is the interpretation we expect with two negative quantifiers. In this respect there is no difference between the semantic status of n-words in Romanian and in DN languages like standard English or German, where DN is the only interpretation for two co-occurring n-constituents. What remains to be explained is the availability of the NC reading.

2.4 Scope properties of negative polyadic quantifiers in NC

Following de Swart and Sag (2002), we analyze determiner n-words and negative NP constituents as quantifiers of Lindström type \(\langle 1,1 \rangle\) and \(\langle 1 \rangle\), respectively (see Lindström (1966)). They may combine by resumption to form a polyadic quantifier of type \(\langle 1^n, n \rangle\) or \(\langle n \rangle\) (van Benthem (1989), Keenan (1992), Keenan and Westerståhl (1997), Peters and Westerståhl (2006)) and thus give rise to an NC interpretation. The negative marker \(nu\) is analyzed as a negative quantifier of type \(\langle 0 \rangle\) that is absorbed under resumption with other polyadic quantifiers.

Before we turn to the specific details of a constraint-based implementation of this general approach in Section 3, we gather additional evidence by considering

\(^6\) The scope disambiguating function of the verbal prefix is reminiscent of the domain restriction effect of modal adverbs that Huitink (2012) describes for modal concord of adverbs and modal verbs in Dutch. However, as Huitink emphasizes, it is unclear if modal concord and NC can be treated analogously under the perspective of polyadic quantification.
related quantificational structures in Romanian. Comparing the scope interaction of Romanian NC constructions with adverbial quantifiers to the scope interaction of a cumulative quantifier with adverbial quantifiers, we observe a remarkable parallelism in the formation of polyadic quantifiers.

The strongest evidence for the presence of polyadic quantification in natural languages comes from examples with peculiar semantic properties. Keenan (1992) focuses on a range of phenomena in natural languages that are known to lie ‘beyond the Frege boundary’, i.e. beyond the expressive power of (iterated) monadic quantifiers. He lists many examples of polyadic quantification which survive a critical review of the older literature on the topic. The sentences (25a) and (25b) from Keenan are transparent examples in which the most natural reading involves an interpretation in which the second quantificational expression (different questions and the same questions, respectively) is not independent of the first. For (25a) this can be seen by considering that the sentence not only asserts that several pupils are in the answering relation with several questions. Crucially, each pupil is in the answering relation with a question that no other pupil chose to answer, making the elements in the second argument slot of the answer relation dependent on the totality of pupils in its first argument, and on the questions they worked on: For each pupil, the set of chosen questions is distinct from the questions answered by any other pupil. If the noun phrases are seen as generalized quantifiers, we can conclude that the formation of a polyadic quantifier is necessary, since no two independent quantifiers can have the intended meaning.⁷

(25) a. Different pupils answered different questions (on the exam).
   b. Every student answered the same questions in the exam.
   c. Forty contributors wrote thirty-two papers.
      i. Each of the forty contributors wrote thirty-two papers.
      ii. Forty contributors wrote each of the thirty-two papers.
      iii. A total of forty contributors wrote a total of thirty-two papers.

In our comparison of clear cases of polyadic quantification with NC we will draw on the Romanian counterpart of (25c), which is ambiguous between three readings, paraphrased in (25c-i)–(25c-iii). The first two readings can be derived by successive application of the two cardinal quantifiers forty contributors and thirty-two papers in different order, and they may involve up to 1280 authors or papers. In the present context, we are especially interested in the third reading, (25c-iii), the so-called cumulative reading, which is also the most prominent interpretation in a neutral context. This last reading shares the property of requiring complex polyadic quantification with (25a) and (25b): Informally, it is again only the totality of all contributors in the first argument slot of the binary write relation that determines the possible members of the second argument slot for each contributor,

⁷ See Barker (2007) for a compositional continuation semantic analysis of same and different as adjectives. Another compelling instance of polyadic quantification is discussed by (Moltmann 1995, p. 260), who argues that the denotation of the exception sentence in (24) involves subtracting the pair (John, Mary) from the set of pairs of men and women.

(24) Every man danced with every woman except John with Mary.
in this case the total number of papers that occur with the set of paper-writing contributors.

The simple symbolization of (25a)–(25c) in a logic with polyadic quantification, (26), illustrates the underlying structure from a representational perspective. In all three cases ((25a), (25b), (25c-iii)), a polyadic quantifier of type \(1^2, 2\) first takes two one-place predicates as restrictors (forming a quantifier of type \(2\)) and then reduces a binary relation to a truth value. The observed dependency between the two arguments in the relation can be formulated because the semantics of the polyadic quantifier affords the expressive power to specify them simultaneously, which cannot be done through the successive application of two monadic quantifiers.

\[(26)\]
\[
a. \quad \text{(different, different)}(\text{pupil, question})(\text{answer}) \\
b. \quad \text{(every, the same)}(\text{student, question})(\text{answer}) \\
c. \quad (40, 32)(\text{contributor, paper})(\text{write})
\]

For the investigation of the quantificational structure of NC we will exploit the Romanian counterpart of (25c), shown in (27), which exhibits the same ambiguity as in English: The notation \((40, 32)\) designates the cumulative reading, while \(40 > 32\) and \(32 > 40\) depict the scope interaction from successive applications of two monadic quantifiers. \(40 > 32\) indicates that \textit{forty contributors outscopes thirty-two papers.}\n
\[(27)\]  
\textbf{Patruzeci de colaboratori} au scris \textbf{treizeci și două de lucrări}. 
\textit{Forty contributors have written thirty-two papers.} 
\[
a. \quad (40, 32) \\
b. \quad 40 > 32 \\
c. \quad 32 > 40
\]

Adding the quantificational adverb \textit{frequently} to a sentence with two cardinals reveals interpretational restrictions, as only a subset of the logically possible scope interactions occur. A connection of the possible readings to NC constructions can be established by replacing the two cardinals with n-constituents and by comparing the putative formation of a negative polyadic quantifier to the configurations in which we observe a cumulative polyadic quantifier with cardinals. The conditions under which we will see cumulation with cardinals will correspond to those in which we assume a polyadic quantifier expressing NC.

In addition to the notational devices introduced above, we use the ampersand when we do not want to commit to a particular reading. \(40 \& 32\) means that the two cardinals either form a polyadic quantifier, \((40, 32)\), or they take individual scope, i.e. \(40 > 32\) or \(32 > 40\). With three quantificational expressions we have to investigate three scenarios: The adverb may take narrowest scope (28a), the adverb may take widest scope (28b), or the adverb is in an intermediate position (28c).

\[(28)\]  
\textbf{Patruzeci de colaboratori} au scris \textit{frecvent treizeci și două de lucrări}. 
\textit{Forty contributors frequently wrote thirty-two papers.} 
\[
a. \quad (40, 32) \\
b. \quad 40 > 32 \\
c. \quad 32 > 40
\]
The interpretation pair (28b-i) and (28b-ii), in which the cardinals are adjacent, and the pair (28c-i) and (28c-ii), in which we test the availability of an intermediate position of the adverb, reveal a remarkable pattern. The first of the two pairs shows that adjacent cardinals receive a cumulative reading (28b-i). This contrasts with the second pair, in which the three quantifiers can only be interpreted with scope interaction, showing that they are monadic quantifiers (28c-ii). A reading in which the cardinals form a polyadic quantifier together with the adverbial is not available (28c-i). Thus it seems that in complex quantificational environments speakers follow a clear strategy of resolving the available interpretation choices: In case the cardinals receive an adjacent interpretation, the polyadic reading prevails. If a third quantifier intervenes, the individual monadic interpretation of all three survives. The readings with reversed scope of the two cardinals in (28b-iii) follows the same pattern.

A slight complication arises with the remaining readings. (28c-iii), in which the adverbial is outscoped by 32 papers, is excluded for the same reason for which no readings with narrow scope of the adverbial are available (28a): To obtain a plausible reading, a different lexical choice of the verb is necessary, re-scrie ‘to re-write’ instead of scrie. With this small modification, (28c-iii) seems possible, as well as the cumulative reading with (40, 32) outscoping the adverbial in (28a). This is consistent with the pattern above.

In (29) we replicate the tests for available readings, with two n-constituents replacing the cardinals. If NC behaves the same way as the cumulative interpretation of two cardinals, we expect an obligatory NC reading when the negative quantifiers are adjacent, and a double negation reading when an adverbial quantifier intervenes. This is in fact what we find:8

(29)  Niciun student nu a citit frecvent nicio carte.
     no   student NM has read frequently no book
     (lit.) ‘No student frequently read no book.’
     a.  NO & NO > FREQ

8 We ignore the negative marker nu, because we already know that it is not interpreted independently in the presence of an n-word but always enters into a concord relation.
The differences that we see in a pairwise comparison to the corresponding interpretation choices in (28) are independent of the pattern concerning the adjacency of the two negative and the two cardinal quantifiers and their interpretation as two monadic or a single polyadic quantifier. Unlike in (28), there is a preference of the negative quantifiers to take wide scope over the adverb. For that reason, (29a-i) is preferred over (29b-i). Given this orthogonal difference, the comparison between (29a-i) and (29c-i) shows that the NC reading is only possible if the two negative quantifiers are adjacent. The pair of (29a-ii) and (29c-ii) indicates that DN arises when the adverb intervenes.

We should stress that the NC character of Romanian causes the DN reading (29c-ii) of sentence (29) to be highly context dependent. It is only really legitimate in a denial context like the one we construct in (30).9 The focus intonation of (30a) ensures that frequently takes wide scope over no book. (30b) denies this reading, yielding the DN interpretation of (29c-ii).

(30) a. A: Am auzit că  Ion n-a citat frecvent  nicio carte.  
    have heard that John NM-has read frequently no book

i.  FREQ > NO: I’ve heard that it was frequently the case that  
    John didn’t read any book.

ii. # NO > FREQ

b. B: NICIun  student nu a citat frecvent  nicio carte.  
    no student NM has read frequently no book

NO (student) > FREQ > NO (book): If a student (sometimes)  
    didn’t read any book, this was not frequent for him/her.

9 Example adapted from Iordâchioaia (2010, p. 102).
We conclude that apart from different scope preferences between monadic quantifiers and different preferences in the relative scope of the polyadic quantifier with respect to the adverbial, the pattern underlying NC and cumulative readings of two cardinals in the presence of the adverbial quantifier frequently is the same. The adjacent interpretation of two potentially polyadic quantifiers is polyadic. If a third quantifier intervenes, their interpretation is monadic.

3 Tools: Polyadic quantifiers and Lexical Resource Semantics

Previous analyses of NC with polyadic quantifiers were proposed in a generative framework by May (1989) and in HPSG by de Swart and Sag (2002). These treatments are implemented by means of an additional layer of syntactic structure (May) or construct resumptive quantifiers with a quantifier retrieval mechanism (de Swart and Sag); they do not address the properties of their syntax-semantics interfaces in light of an elaborate notion of semantic compositionality. The main challenge for a technically precise implementation is that resumption of quantifiers, for example the formation of a binary quantifier out of two monadic quantifiers, cannot in general be expressed by a compositional semantic operation in a functional type theory. However, the observations on Romanian NC in the previous section suggest that this type of logical analysis is what we need for an adequate description of the data: Whenever we can test their semantic import, single n-words have the properties of negative quantifiers. Multiple n-words in a sentence behave like a single negative polyadic quantifier (unless they are interpreted as individual negative quantifiers). Standard semantic theories of linguistics with composition mechanisms such as function application of the logical translation of one syntactic daughter to the translation of the other cannot do justice to both observations at the same time. Indeed, they cannot construct polyadic quantifiers at all.10

This is where we turn to an alternative, systematic theory of the syntax-semantics interface that can give us exactly what we need, viz. a standard logical interpretation of natural language expressions, a translation of Romanian nimeni ‘nobody’ and corresponding quantificational expressions as negative quantifiers, and the potential formation of a polyadic negative quantifier from several lexical negative quantifiers in clearly specified syntactic environments. A constraint-based theory of semantic composition from the family of semantic underspecification formalisms can do this for us. We choose a member of this family of representation and composition formalisms that is very precise about its logical object languages, and supports the construction of a polyadic quantifier in the presence of lexical negative quantifiers directly by underspecification, without the necessity of integrating a resumption operator in the logical language. As a result, we will obtain elegant general specifications, and transparent logical translations of Romanian sentences.

To sum up our shopping list, for our analysis of Romanian NC with polyadic quantifiers we need two ingredients: A higher-order logical object language for expressing the truth conditions of sentences with NC constructions, and a semantic

10 For an argument why this fails even for the simplest mode of polyadic composition, iteration, which corresponds semantically to function application, see (Iordăchioaia 2010, pp. 142–146). The reason that compositionality fails for iteration is that the syntax of natural language does not appropriately map on the syntax of a logical language with iteration.
composition theory which derives the intended expressions from lexical semantic specifications and the syntactic structure of our sentences. As logical object language we use a straightforward extension of two-sorted type theory (Ty2, Gallin (1975)) by negative polyadic quantification (Section 3.1); the theory of semantic composition is taken from LRS (Richter and Sailer (2004); Richter and Kallmeyer (2009)), which gives us a system of constraints for semantic composition and a format for lexical specifications, as well as an interface to syntactic structures in HPSG (Section 3.2). Only minimal adjustments are necessary to accommodate polyadic quantification in this system. For convenience we briefly restate all relevant LRS principles from the literature, and conclude with a simple example of semantic composition in Section 3.3.

3.1 The logical object language

We assume a simple theory of types with types $e$ (for entities), $s$ (for world indices) and $t$ (truth values). Functional types are formed in the usual way. The syntax of the logical language provides function application, lambda abstraction, equality and negative polyadic quantifiers. By standard results this is enough to express the usual logical connectives and monadic quantifiers. In reference to the simple type theory and the close relationship to Gallin (1975), we call our family of languages Ty2. For simplicity, polyadic negative quantification is introduced syncategorematically.\footnote{The syntax underlying our LRS implementation will treat it as a family of constants. For that reason, we refer to our logical languages as Ty2, although strictly speaking the present definition presents Ty2 augmented by syncategorematic polyadic quantifiers.} $\text{Var}$ and $\text{Const}$ are a countably infinite supply of variables and constants of each type:

**Definition 1** Ty2 Terms: $\text{Ty2}$ is the smallest set such that:

- $\text{Var} \subseteq \text{Ty2}$, $\text{Const} \subseteq \text{Ty2}$,
- for each $\tau, \tau' \in \text{Type}$, for each $\alpha_{\tau, \tau'}, \beta_{\tau} \in \text{Ty2}$:
  - $(\alpha_{\tau, \tau'}, \beta_{\tau})_{\tau'} \in \text{Ty2}$,
- for each $\tau, \tau' \in \text{Type}$, for each $i \in \mathbb{N}^+$, for each $v_{i, \tau} \in \text{Var}$, for each $\alpha_{\tau'} \in \text{Ty2}$:
  - $(\lambda v_{i, \tau}. \alpha_{\tau'})_{(\tau', \tau')} \in \text{Ty2}$,
- for each $\tau \in \text{Type}$, and for each $\alpha_\tau, \beta_\tau \in \text{Ty2}$:
  - $(\alpha_\tau = \beta_\tau)_t \in \text{Ty2}$,
- for each $\tau \in \text{Type}$, for each $n \in \mathbb{N}^+$, for each $i_1, i_2, ..., i_n \in \mathbb{N}^+$, for each $v_{i_1, \tau}, v_{i_2, \tau}, ..., v_{i_n, \tau} \in \text{Var}$, for each $\alpha_{t_1}, \alpha_{t_2}, ..., \alpha_{t_n}, \beta_t \in \text{Ty2}$:
  - $(\text{NO}(v_{i_1, \tau}, ..., v_{i_n, \tau})(\alpha_{t_1}, ..., \alpha_{t_n})(\beta_t))_t \in \text{Ty2}$.

Our syntactic notation for the family of negative polyadic quantifiers (which bind $n$ variables of arbitrary but identical type $\tau$) is motivated by the function of variables in LRS as handles for syntactic arguments of natural language predicates. For convenience we assume that the number of variables $(v_{i_n, \tau})$ corresponds to the number of restrictors $(\alpha_{tn})$ of each quantifier, with $\beta_t$ the nuclear scope of the quantifier. In our fragment of Romanian, the restrictors will come from the head
nouns of generalized quantifiers in syntactic argument positions of verbs, and the nuclear scope will essentially be the translation of the verbal predicate itself.

The standard constructs (function application, lambda abstraction, and equality) receive their usual interpretation. Here we only state the interpretation of negative polyadic quantifiers:

**Definition 2** The Semantics of Ty2 Terms

(clause for negative polyadic quantifiers only)

For each model $M$ and for each variable assignment $a$ in $\text{Ass}$, for each $\tau$ in $\text{Type}$, for each $n$ in $\mathbb{N}^0$, for each $i_1, i_2, \ldots, i_n \in \mathbb{N}^+$, for each $\nu_1, \tau, \nu_2, \tau, \ldots, \nu_n, \tau \in \text{Var}$, for each $\alpha_{i_1}, \alpha_{i_2}, \ldots, \alpha_{i_n}, \beta_t \in \text{Ty}_2$:

$$\lfloor \text{NO}(\nu_1, \tau, \ldots, \nu_n, \tau)(\alpha_{i_1}, \ldots, \alpha_{i_n})(\beta_t) \rfloor^M, a = 1 \text{ iff for every } d_{i_1}, d_{i_2}, \ldots, d_{i_n} \in D_{E, \tau},$$

$$\lfloor \alpha_{i_1} \rfloor^M, a[\nu_1, \tau/d_{i_1}] = 0 \text{ or } \lfloor \alpha_{i_2} \rfloor^M, a[\nu_2, \tau/d_{i_2}] = 0 \text{ or } \ldots \text{or} \lfloor \beta_t \rfloor^M, a[(\nu_1, \ldots, \nu_n)/(d_{i_1}, \ldots, d_{i_n})] = 0.$$

Intuitively speaking, this says that an expression with a negative quantifier with $n$ restrictors can only be true in a model $M$ with respect to a variable assignment $a$ if for each $n$ tuple of objects $d_i$ of the appropriate type, either (1) at least one of the restrictors $\alpha_{i_1}$ does not hold of its corresponding object $d_{i_1}$, or (2) the nuclear scope $\beta_t$ does not hold of the $n$-tuple of objects. In other words, either it is not an $n$ tuple of the kind we are interested in, or the main predicate of the sentence does not hold of it (or both).

(31) illustrates how the definitions are put to use for sentences with NC and sentential negation by stating the truth conditions we obtain for the intended logical specifications of the Romanian literal counterparts of *John didn’t come* (31a) and *No teacher didn’t give no book to no student*, where all NPs are n-constituents and form a ternary negative quantifier by resumption (31b):\(^{12}\)

\[
\begin{align*}
(31) & \quad \text{a. Ion nu a venit.} \\
& \quad \text{For } n = 0, \\
& \quad \lfloor \text{NO}()()\rfloor^M, a = 1 \text{ iff } \lfloor \text{come}'(\text{john}') \rfloor^M, a = 0 \\
& \quad \text{b. Nicium profesor nu a dat nicio carte niciumui student.} \\
& \quad \text{For } n = 3, \nu_{i_1} = x, \nu_{i_2} = y, \nu_{i_3} = z, \alpha_{i_1} = \text{teacher}'(x), \alpha_{i_2} = \text{book}'(y), \alpha_{i_3} = \text{student}'(z) \text{ and } \beta_t = \text{give}'(x, y, z), \\
& \quad \lfloor \text{NO}(x, y, z)(\text{teacher}'(x), \text{book}'(y), \text{student}'(z)) \text{ (give}'(x, y, z)) \rfloor^M, a = 1 \text{ iff for every } d_1, d_2, d_3 \in D_{E, e}, \\
& \quad \lfloor \text{teacher}'(x) \rfloor^M, a[x/d_1] = 0 \text{ or } \lfloor \text{book}'(y) \rfloor^M, a[y/d_2] = 0 \text{ or } \\
& \quad \lfloor \text{student}'(z) \rfloor^M, a[z/d_3] = 0 \text{ or } \\
& \quad \lfloor \text{give}'(x, y, z) \rfloor^M, a[(x, y, z)/(d_1, d_2, d_3)] = 0
\end{align*}
\]

(31a) is an example of a quantifier of Lindström type (0), which corresponds to classical negation. The negative polyadic quantifier in (31b) corresponds to a

\(^{12}\) Initially we will not employ the type $s$ of possible worlds in our representations. Possible worlds will be added in Section 5.
quantifier of Lindström type $⟨1^3, 3⟩$, i.e. it can be read in the given context as reducing three unary relations (the restrictors) and a ternary relation (the predicate $\text{give}'$), and returning a truth value. Note that in the Lindström classification, a determiner quantifier such as $\text{most}$ is of type $⟨1, 1⟩$ (reducing two relations, restrictor and nuclear scope, by one argument), and a generalized quantifier such as $\text{every student}$ is of type $⟨1⟩$ (reducing a relation, the nuclear scope, by one argument).

3.2 Basics of Lexical Resource Semantics

LRS is a constraint-based semantic composition theory built around the leading intuition that a system of constraints governs the combinability of lexical semantic contributions depending on the syntactic structure in which they participate. Approaching the LRS architecture by way of an introductory simile, semantic composition can be thought of as solving a jigsaw puzzle: All words in an utterance contribute their semantics in terms of (potentially several pieces of) typed logical expressions to an unstructured repository of expressions from which the semantics of the utterance must be composed. The words thus provide all the semantic resources of an utterance, or the pieces of the puzzle. Just as with a jigsaw puzzle, the task is to determine in which way the pieces in the bag fit together to form a coherent whole. The logical types of the formal expressions are a first layer of restrictions that correspond to the tabs and blanks of puzzle pieces. But in addition to the type-determined shapes of the contributed pieces, an additional set of restrictions on permissible combinations enters the scene: the constraint system of the semantic theory (which could be conceived of as the picture printed on the pieces). Fundamental constraints are triggered by the syntactic structure that is responsible for the ways in which words and phrases are combined. These constraints are reminiscent of a classical semantic translation function that works in tandem with syntactic rules. Its constraint-based counterparts decree, depending on the kind of syntactic configuration of signs, which restrictions the combination of their semantic translation must obey. For example, when a determiner such as $\text{three}$ syntactically combines with a noun such as $\text{students}$, the logical translation of the noun must occur in the restrictor of the logical translation of the determiner. The set of all combinatoric constraints (triggered by phrase structure and other criteria) together with the shapes of logical expressions that were collected in the bag of resources contributed by the lexical elements in the utterance, determine how the pieces may be combined to yield a well-formed logical translation of the utterance. Note that, in contrast to simple traditional jigsaw puzzles, more than one legitimate well-formed picture may emerge: utterances may be semantically ambiguous, even for a single syntactic analysis.

Finally, for NC one more property of LRS plays a major role, which does not have a counterpart in jigsaw puzzles: If two words contribute semantic expressions of the same shape, it might turn out (by means of the constraint system) that these expressions are not only of the same shape, they are one and the same expression. This means that the semantic contribution of two negative polyadic quantifiers by two $n$-words can potentially be resolved to a single negative polyadic quantifier of the appropriate arity. However, since the relevant constraints of Romanian are not always deterministic, semantic underspecification may permit more than one solution for NC constructions: Two lexically underspecified negative polyadic
quantifiers, contributed by two n-words, may legitimately form a binary negative quantifier; or they may be conceived of as two distinct monadic negative quantifiers, one outscoping the other. By contrast, Romanian is strict about the behavior of finite verbs in the presence of an n-word. The presence of an underspecified polyadic quantifier contributed by an n-word leads to the requirement that the finite verb be negated and the contingent negative quantifier at the verb enter NC with a polyadic quantifier.

Summarizing our high-level characterization of the present approach, what is at work in the LRS account of Romanian NC are by and large three components of the semantic composition theory: underspecified semantic contributions of words (the lexical resources); a very general strategy of indiscriminately collecting all these contributions in a sentence, generating a large space of possible readings (a bag of lexical resources for a given utterance); and a set of constraints whose job it is to filter the space of possible readings in order to narrow it down to the actual readings of the sentence (the set of semantic constraints applied to a given syntactic structure).

Let us now take a closer look at how the above program is carried out. In order to feed the constraint system, LRS distinguishes several aspects of the semantics of a sign, of which we single out five that are immediately relevant for our purposes: (1) its semantic contribution, expressed through a list-valued feature parts, which records which components of the semantic term of an utterance are contributed by that sign, (2) the internal content of a sign (value of the attribute incont), which distinguishes the part of the term that will be outscoped by any other operator with which the sign combines within its syntactic projection, (3) the external content of a sign (value of the attribute excont), which is the term formed at the maximal syntactic projection of the sign, (4) the var value of local semantics, by which semantic functors gain access to logical variables provided by their arguments, and (5) the main value of the local semantics, which contains the main semantic contribution of lexical signs, e.g. the lexical semantic predicate of verbs or nouns.

The two descriptions in (32a) and (32b) illustrate these distinctions with two syntactic categories relevant to our discussion, the head noun of an NP, studenți ‘students’, and the corresponding NP node, trei studenți ‘three students’.

(32) a.  

```
word phon ss|loc  
cont excont incont sem

studenti  
head noun  
val spr (DETf [f])  
index [var 5a student]  
main 5a student  
parts ([2 student ([4a], 5a student)])
```
The local content of the noun `studenți` (under the LOC(AL) attribute, and therefore available for syntactic-semantic selection by valence features in HPSG) consists of its main content, the nonlogical constant `student'` and a variable, designated by the tag \(4a\). The tag notation indicates that the variable originates from the syntactic determiner the noun selects by means of one of its VAL(ENCE) features, (DetP\(4a\)). The fact that the variable does not come from the noun can be confirmed by investigating the noun’s combinatoric semantics, contained in the lrs structure under the SEM(ANTICS) attribute: The parts list enumerates the semantic lexical resources contributed by the noun. These are two objects, the nonlogical constant `student'`, indicated by tag \(3a\), and the application of `student'` to an argument, \(3\). The variable, \(4a\), is not an element on the list of contributed resources.\(^\text{13}\) The internal content of the noun consists of the nonlogical constant applied to its argument (which will be outscoped by any scope taking element in the noun’s syntactic projection), and the external content must be a generalized quantifier. By this specification, the nominal head already determines that its maximal projection must denote a quantifier.

(32b) shows a nominal phrase that is the maximal syntactic projection of the previous noun. As will be explained below, a syntactic projection shares the local semantic values with its head as well as the INCONT and EXCONT values. As to the semantic resources, the nominal phrase `trei studenți` comprises the previously discussed resources of `studenți` plus the resources contributed by the generalized quantifier. The quantifier contributes the variable \((x)\), the quantifier symbol `three`, and applications to its arguments, all designated by tags starting with the integer 4. Finally, the AVM in (32b) is conjoined with a subterm constraint, \(\mathbf{4} \triangleleft \gamma\). This constraint says that the expression `student'(x)`, designated by \(\mathbf{4}\), must be a (possibly improper) subterm of the restrictor, \(\gamma\), of the generalized quantifier. A stronger statement to the effect that `student'(x)` equals the restrictor of the quantifier is potentially false, because further syntactic material (such as an extraposed relative clause) might introduce additional semantic restrictions on the set of students inside the restrictor.

Contributions to the semantics of utterances are exclusively and exhaustively made by the lexical items in the utterance. Phrases do not contribute meaning components, they only trigger restrictions, expressed in the SEMANTICS PRINCIPLE, which constrain how the semantics of their immediate syntactic daughters

\(^{13}\) We follow the notational convention in the LRS literature of grouping related resources by tags with the same integer: In the present examples, the contributions of `studenți` are designated by 3, the contributions of `trei` by 4, followed by lower case letters.
can be put together.\footnote{As one reviewer remarks, this strategy of purely lexicalized semantic resources seems at odds with work in Construction Grammar that assumes semantic effects of constructions in addition to the words that occur in them. The apparent incompatibility of these assumptions is weaker than it appears: Work in LRS also assumes phrasal lexical entries, which license phrases that contribute semantic resources because they are conceived of as complex lexical items. The theory of idiomatic phrases and phraseological clauses of Richter and Sailer (2009) develops central aspects of this approach and compares it to Sign-based Construction Grammar. A detailed discussion is beyond the scope of the present paper.} Two such clauses of the Semantics Principle that we introduce below in (36) and (37) will dictate that when a determiner quantifier together with a nominal projection forms a nominal phrase, the semantics of the noun projection must be in the restrictor of the quantifier that comes from the determiner; and when a generalized NP quantifier combines as a syntactic argument with a verb projection, the semantics of the verbal head of the VP must be in the nuclear scope of the generalized quantifier. The internal and external contents of the phrase and of its daughters are instrumental in stating constraints like these, together with the subterm relation ($\alpha \preceq \beta$). Later we will see a generalization of the subterm relation to the form $\alpha \preceq \vec{\nu}$, where $\alpha$ is a term, $\vec{\nu}$ is a vector of terms, and $\alpha$ must be a (possibly improper) subterm of one of the terms in $\vec{\nu}$.

LRS principles express restrictions on terms of a logical object language (in our case: terms of Ty2), i.e. they are written in a meta-language whose expressions denote terms of Ty2. For reasons of convenience and readability, the expressions of the meta-language partially look like the object language itself, adding metavariables and additional syntactic constructs such as the notation for subterm constraints. To avoid confusing different levels of denotation, it is important to keep in mind that LRS meta-language expressions such as $\text{come}'(\text{john}')$ are descriptions of object language terms, in this case of the Ty2 expression of the same form.\footnote{For mathematical details of how object languages such as Ty2 can be specified in a feature logic for HPSG, see Sailer (2003); Penn and Richter (2004, p. 426–429) present a feature logical signature and a set of axioms of LRS that can easily be extended to capture the version of Ty2 with polyadic quantification we use here.}

Before discussing a simple example of deriving the semantics of a phrase, let us briefly review three standard LRS principles that underlie the present version of our constraint-based semantic framework.\footnote{We follow the most recent version of LRS presented in Richter and Kallmeyer (2009).} These are the LRS Projection Principle, the Incont Principle and the Excont Principle. The LRS Projection Principle governs the relationship of the attribute values of excont, incont and parts at phrases relative to their syntactic daughters. It is responsible for the excont and the incont identity along syntactic head projections, and for the inheritance of the elements of parts lists by phrases from their daughters:

\begin{equation}
\text{(33) LRS Projection Principle (Richter and Kallmeyer 2009, pp. 47–48)}
\end{equation}

In each phrase,
1. the excont values of the head and the mother are identical,
2. the incont values of the head and the mother are identical,
3. the parts value contains all and only the elements of the parts values of the daughters.

The Incont Principle and the Excont Principle constrain the admissible values of the incont and the excont attribute in syntactic structures. The Incont Principle is the simpler one of them. It guarantees two things: First,
the internal content of a sign (the part of its semantics that is outscoped by any operator the sign combines with along its syntactic projection) is always semantically contributed by the sign, i.e. it is a member of its parts list. And second, the internal content is in the external content of a sign. In a first approximation (which is precise enough for our purposes) this means that the internal content contributes its semantics within the maximal syntactic projection of a sign.

(34) The Incont Principle (Richter and Kallmeyer 2009, p. 47)  
In each lrs, the incont value is an element of the parts list and a component of the excont value.

The Excont Principle is slightly more complex. Its first clause requires that the external content of a non-head daughter be semantically contributed from within the non-head-daughter. The second clause is a closure principle and says that the semantic representation of an utterance comprises all and only those pieces of semantic representations that are contributed by the lexical items in the utterance.

Clause 1:  
In every phrase, the excont value of the non-head daughter is an element of the non-head daughter’s parts list.  
Clause 2:  
In every utterance, every subexpression of the excont value of the utterance is an element of its parts list, and every element of the utterance’s parts list is a subexpression of the excont value.

As stated above, we follow the usual notational conventions and write descriptions of expressions of the semantic representation language as (partial) logical expressions. For describing polyadic quantifiers we use the notation \( Q(\vec{v}, \vec{\phi}, \psi) \). Here \( \vec{v} \) and \( \vec{\phi} \) are shorthand for a (possibly empty) vector of variables and a (possibly empty) vector of expressions; \( \psi \) is a single expression. In the analysis of Romanian below we will assume that there is an appropriate subsort of gen-quantifier in our grammar which is interpreted as negative polyadic quantifier. In our notation this family of quantifiers will be denoted by \( no(\vec{v}, \vec{\phi}, \psi) \).

In addition to the core principles of the attributes excont, incont and parts, LRS offers a set of constraints that are collected in the clauses of the Semantics Principle. The clauses of the semantics principle concern phrasal syntactic structures and make statements about the relationship between (subterms of) the excont and the incont values of phrases of a particular syntactic type and their daughters. These are the restrictions of how the semantic contributions of the daughters fit together and may be combined at the mother node. If the restrictions are not very specific, they might allow different ways of putting the pieces together: The readings we obtain at the mother node are underspecified.

The clause of the Semantics Principle governing the combination of quantificational determiners with nominal heads has to be adjusted to polyadic quantifiers. The relevant clause is shown in (36). Except for the generalization from monadic quantifiers to polyadic quantifiers, it is identical to the corresponding clause in (Richter and Kallmeyer 2009, p. 65).
The Semantics Principle, Clause 1
If the non-head is a quantifier, then its incont value is of the form $Q(\vec{v}, \phi, \psi)$, the incont value of the head is a component of a member of the list $\phi$, and the incont value of the non-head daughter is identical to the excont value of the head daughter.

One more clause of the Semantics Principle will become relevant in Section 4 when we combine noun phrase quantifiers with the verb phrase which subcategorizes them. Here is the semantic constraint which must hold for these syntactic structures, generalized from standard formulations to the case of polyadic quantification:

The Semantics Principle, Clause 2
If the non-head is a quantified NP with an excont value of the form $Q(\vec{v}, \phi, \psi)$, then the incont value of the head is a component of $\psi$.

With the integration of polyadic quantifiers and the modified clauses of the Semantics Principle we have completed the adjustments in LRS needed to formulate our theory of NC. Resumption will be implemented in LRS as identity of quantifiers contributed by lexical elements, and there is no need to add a resumption operator to the logical language. For that reason no special technical apparatus for the resumption operation has to be introduced in preparation of our analysis of negative concord in Romanian. We conclude the discussion of LRS with a simple example in Section 3.3.

Among the most salient properties of LRS is its capability to provide under-specified descriptions of sets of meanings, and its use of subterm constraints. In this respect it is very similar to other frameworks of underspecified semantics, including Minimal Recursion Semantics (MRS, Copestake et al. (2005)) and the Constraint Language for Lambda Structures (CLLS, Egg et al. (2001)). While MRS is also typically used in a feature logic encoding in HPSG and serves as

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17 Recall that the relation `$\subseteq$` is a generalized subterm relation derived from `$\in$`, denoting subtermhood on lists of terms, e.g. $t_2 \subseteq (t_1, (t_2 \land t_3), t_4)$.

18 For readers familiar with the formal specification language of HPSG constraints, the following AVM formula makes the logical structure of the principle transparent:

$$\forall [dtrs | spr-dtr|ss | loc | cat | head | det | main | gen-quantifier | restr] \rightarrow$$

$$\exists [h-dtr | sem | excont | incont | gen-quantifier | restr | \phi] \land \phi \subseteq \phi$$

In formal notation:

$$\forall [dtrs | spr-dtr|ss | loc | cat | NP | restr | gen-quantifier] \land non-hd-dtr(\phi, \phi)$$

$$\rightarrow [dtrs | h-dtr | sem | incont | \phi] \land \phi \subseteq \phi$$

Here, non-hd-dtr is a binary relation that identifies the non-head daughter of a phrase. The use of the relation makes it possible to stay agnostic with respect to exact phrase type and to the attributes that encode the non-head daughter.
a widely used meta-language framework for semantic representations in computational environments, LRS emphasizes the specification of concrete higher-order logical object languages for the investigation of semantic distinctions for which the exact truth conditions of linguistic expressions matter. CLLS shares the idea of embedding standard logical languages of linguistic semantics with LRS. At the same time there is one crucial feature that distinguishes LRS from MRS, CLLS, and all other underspecification frameworks we are aware of, which is the strategy of permitting multiple lexical sources of one and the same meaning contribution to an utterance. We will see that this property plays an indispensable role in our polyadic analysis of NC.

3.3 An example

With the principles in the previous section everything is in place to explain the LRS analysis of the semantic composition in a simple clause with a generalized quantifier in subject position (Fig. 1). As throughout this paper, we ignore tense.

The words at the leaves of the syntactic tree reveal the lexical semantic specifications of determiners, count nouns and verbs. The noun *studenți* ‘students’ expects a generalized quantifier in its maximal projection (EXCONT value). Its internal content is *student*′(*x*), the application of the constant *student*′ of type ⟨e, t⟩ to a variable of type e. The variable is known to the word *studenți* because as a noun it selects its determiner via its spr list20, where it has local access to the variable. The PARTS list shows that the word *studenți* contributes the constant *student*′ and its application to *x* to the semantics of the utterance. The determiner

---

20 For simplicity, the var attribute is not shown in Figure 1; (32a) above contains the complete LRS specification with determiner selection and local var and main values of the word.
trei ‘three’ contributes the monadic quantifier _three_ (of type \( (1,1) \)), the variable _x_, and the applications of the quantifier to its restrictor and scope. The internal and the external content of _trei_ is the generalized quantifier, whose restrictor and scope are not known in the lexicon. They are given in terms of two meta-variables, \( \gamma \) and \( \delta \). The verb _au venit_ ‘came’ looks similar to a count noun, except that it imposes no restriction on the external content at the lexical level: The verb contributes the constant _come_’ of type \( (e,t) \) and its application to an argument of type \( e \). Parallel to the situation in nominal projections, the verb has access to that argument through the syntactic selection of the subject by a valence feature. In the present example, the var value of the subject is the variable _x_ (see (32b)).

The lexical semantic resources of the quantifier, the noun and the verb (typed terms plus some information on which functor applies to which argument) are the material that the LRS constraints work on to determine the possible _excont_ values of the sentence. In our simple example they will lead to a single reading. The LRS principles determine the semantics of the NP based on the lexical semantic contributions of the determiner and the noun, and on the syntactic fact that a determiner is syntactically combined with a nominal head: The semantic contributions of the two daughters are collected in the _parts_ list of the NP mother, and internal and external content are inherited from the syntactic head daughter, which is the noun (LRS Projection Principle). Clause 1 of the Semantics Principle demands that the incont of the determiner be equal to the _excont_ of _studenti_ and that the incont of the head daughter, _student_’(x), be a subterm of the restrictor of the generalized quantifier. The semantics of the NP is thus given by the constraints on the _excont_ of the NP: It is the generalized quantifier _three_ binding the variable _x_, with _student_’(x) in the restrictor and as yet unknown nuclear scope. The scope of the quantifier is determined when the NP combines with the verb to form the sentence: The verb is the syntactic head of the construction, which is why the incont and _excont_ of the verb and the sentence node are identical; all elements from all parts lists are collected on the parts list of the sentence (LRS Projection Principle). The semantics of a syntactic combination of a nominal generalized quantifier with a verbal projection is restricted by Clause 2 of the Semantics Principle, which demands that the incont of the verb, _come_’(x), be a subterm of the nuclear scope, \( \delta \), of the quantifier. This is indicated in Fig. 1 by the subterm constraint \( \bullet \ll \delta \), notated next to the AVM at the S node.

Finally, the Excont Principle decrees that the external content of the NP must be contributed from within the NP (which it is, as it comes from _trei_), and that the excont value of the complete utterance must be constructed from all contributions of all the words in it. Of course, that value must respect all constraints that are imposed on the possible combination of all terms. In particular, _student_’(x) must be in the restrictor and _come_’(x) must be in the scope of the quantifier. The only term which respects these conditions (and is a well-formed term) is the one shown as _excont_ value of the sentence in Fig. 1.

4 The analysis of Romanian NC

We will proceed in several steps, with the main plot developing in the first two sections: In Section 4.1 we lay out the analysis of sentential negation with the
4.1 Sentential negation

The analysis of simple negated clauses without n-constituents like (3a) follows immediately from the lexical analysis of verbs with the NM prefix nu. The affixal nature of nu is extensively argued for in Barbu (2004). Following assumptions similar to ours in Ionescu (1999) and the parallel analysis of the Polish negative marker in Przepiórkowski and Kupść (1997), we formulate the lexical rule in (38), which relates each verb form of the appropriate kind to a corresponding negated form.

\[
(38) \quad \text{The NM Lexical Rule}
\]

\[
\begin{array}{c}
\text{word} \quad \text{nu} \\
\text{PHON} \\
\text{SS|LOC|CAT} \quad \text{HEAD} \quad \text{vform} \quad \text{fin} \vee \text{inf} \\
\text{SEM} \quad \text{excont} \quad \text{incont} \quad \text{parts} \quad \text{nu} \quad \text{unmarked} \\
\wedge \neg \exists \text{no}(\vec{u}, \vec{\alpha}, \vec{\beta}) \equiv \text{nu}
\end{array}
\]

\[
\begin{array}{c}
\text{PHON} \quad f_{\text{neg}}(\text{nu}) \\
\text{SS|LOC|CAT|HEAD} \quad \text{nu} \quad \text{NM} \\
\text{SEM} \quad \text{parts} \quad \text{nu} \quad \text{expletive} \\
\wedge \exists \equiv \delta \wedge \exists \equiv \rho
\end{array}
\]

The NM attaches to finite and infinitival verb forms as indicated by the vform value in (38). The feature nu has three values (unmarked, NM, and expletive), and ensures that nu is attached to a verb only once. All verb forms in the (base) lexicon are specified as [nu unmarked] and may have a [nu NM] counterpart only if they undergo this lexical rule. The value [nu expletive] is reserved for expletive negation, on which we briefly comment below. The function \( f_{\text{neg}} \) in the phon value description of the output encodes a phonological rule and is responsible for the correct phonological forms with the verbal prefix. It permits reduction of nu to n– depending on the first phoneme in the input’s verb form.

The semantic counterpart to the negative prefixation by nu in the phonological form is a negative quantifier on the parts list of the originally positive verb (note that the input must lack a negative quantifier). The interpretation of the verb form
as negated is a consequence of the requirement that the internal content of the verb \( t \) be a subterm of the nuclear scope \( \delta \) of this quantifier \( \left( t \equiv \delta \right) \) in the output description of the lexical rule). The negative quantifier \( x \) is also a subterm of the external content \( \psi \) of the verb \( \left( x \equiv \psi \right) \). This condition will become important in the analysis of embedded clauses in Section 5 and will be responsible for the inability of the negation on an embedded verb form to outscope a matrix verb. As discussed below, negative quantifiers contributed by embedded clause n-words in argument position will, under certain conditions, have the additional option of taking a scope that includes the matrix clause.

The negative verb form \( nu \ a \ venit \) in our sentence (3a) is licensed as output of the NM Lexical Rule and is shown below:

\[
\begin{align*}
\text{(39)} & \quad \text{nu a venit ('NM has come', licensed by the NM Lexical Rule)} \\
& \quad \begin{cases}
\text{word} & \langle \text{nu, a, venit} \rangle \\
\text{phon} & \langle \text{nu, a, venit} \rangle \\
\text{ss} & \langle \text{nu, a, venit} \rangle \\
\text{loc} & \langle \text{nu, a, venit} \rangle \\
\text{cat} & \langle \text{head|nu, val|NM, subj|NP} \rangle \\
\text{index} & \langle \text{var|no-var, main|nu|come'} \rangle \\
\text{cont} & \langle \text{excont|nu, incont|come', parts|nu, a, venit} \rangle \\
\text{sem} & \langle \text{excont|nu, incont|come', parts|nu, a, venit} \rangle \\
\end{cases}
\end{align*}
\]

With standard LRS mechanisms we obtain the two readings available for the ambiguous sentence in (3a): \( \text{three}(x, \text{student'}(x), \text{no}()(), \text{come'}(x)) \), where \( \text{three} \) takes scope over \( \text{no} \), and \( \text{no}()(), \text{three}(x, \text{student'}(x), \text{come'}(x)) \), where the NM outscopes the cardinal quantifier. The variable and restrictor lists of the negative quantifier are empty (Lindström type \( \langle 0 \rangle \)) because the negative verb does not introduce a variable, and the sentence does not provide a restrictor.

4.2 NC constructions

Determiner n-words contribute negative quantifiers of underspecified Lindström type \( \langle 1^n, n \rangle \). In their LRS representation they lexically contribute exactly one new variable, which means that they contribute a Lindström quantifier \( \langle 1^n, n \rangle \) with \( n \geq 1 \). The (relevant part of the) lexical entry of the determiner \textit{niciun} exemplifies this pattern (40a). Unlike the negated verb in (39), \textit{niciun} introduces a variable \( (x) \), and the negative quantifier \( \text{no}(\vec{v}, \vec{\alpha}, \vec{\beta}) \) binds \( x (x \in \vec{v}) \). In addition, the variable is a subterm of the nuclear scope \( (x \equiv \vec{\alpha}) \) and a subterm of a member in the restrictor list of the quantifier \( (x \equiv \vec{\alpha}) \). These conditions guarantee the existence of a restrictor and prevent empty quantification.
With the lexical entries of the determiner and the noun we have all necessary ingredients to investigate simple NC constructions with one n-word like sentence (3b). The relevant parts of the structure are shown in Figure 2.

According to the LRS Projection Principle, the NP inherits the incont value \( \bar{\alpha} \) of its nominal head. Due to the first clause of the Semantics Principle the internal content must be a subterm of a member of the restrictor list of the quantifier \( \bar{\alpha} \). The excont value is identified with the incont value \( \bar{\alpha} \) of the determiner due to the interaction of the first clause of the Excont Principle with the other restrictions on the excont of the NP. At the S node of the sentence two more restrictions become relevant. All lexically introduced pieces of semantic representation must be realized in the excont of the sentence, including the excont of the NP and the negative polyadic quantifier from the parts list of the verb \( \bar{\alpha} \). Moreover, the standard clause of the LRS Semantics
**Principle** for combining NP-quantifiers in argument position with verbal projections requires that the polyadic quantifier of the NP take scope over the verb \( \varrho \triangleleft \beta \).

All these restrictions together license three distinct expressions in the \textsc{excont} of the sentence. Only one of them, shown in (41a), corresponds to the linguistic facts, the other two result from possible scope interactions of the negative quantifier of the verb and the NP-quantifier. The NC reading (41a) obtains if the two negative quantifiers get identified, meaning that \( \varrho = \varrho, \vec{v} = \vec{u} = x, \vec{a} = \vec{\gamma} = \text{student}'(x), \) and \( \beta = \delta = \text{come}'(x) \).

\[
\begin{align*}
\text{(41)} & \quad \text{a. } \text{no}(x, \text{student}'(x), \text{come}'(x)) \; \varrho = \varrho = \varrho \\
\text{b. } \text{no}(x, \text{student}'(x), \text{no}(), (), \text{come}'(x)) \; \varrho = \varrho : \delta = \beta = \varrho \\
\text{c. } \text{no}(), (), \text{no}(x, \text{student}'(x), \text{come}'(x)) \; \varrho = \varrho : \delta = \beta = \varrho
\end{align*}
\]

(41b) and (41c) are impossible DN readings of (3b) and have to be excluded by the theory of Romanian NC. At the same time we have to take care that an n-word in a sentence obligatorily triggers the NM on the finite verb. We achieve both goals in one step by adapting the \textsc{Neg Criterion} for Polish of Richter and Sailer (2004) to Romanian and the polyadic quantifier approach.

\[
\text{(42) The Neg Criterion for Romanian} \]

If a negative quantifier of type higher than \( \langle 0 \rangle \) outscopes a finite verb within the verb’s external content, then the \textsc{parts} list of the verb must contain a negative quantifier of type higher than \( \langle 0 \rangle \).\(^{21}\)

Intuitively, the \textsc{Neg Criterion} says that the presence of an n-word in a sentence requires the presence of a (possibly different) n-word that undergoes resumption with the NM on the verb. More precisely, the \textsc{Neg Criterion} is sensitive to the presence of a negative quantifier of a type higher than \( \langle 0 \rangle \) in the \textsc{excont} of a finite verb (contributed by at least one n-word). In that constellation a negative quantifier of type higher than \( \langle 0 \rangle \) must also be on the \textsc{parts} list of the verb. Since those verbs that are licensed by lexical entries do not carry negative quantifiers in their \textsc{parts} lists, this means that only verbs licensed by the NM \textsc{Lexical Rule} are eligible. But since the quantifier contributed by a negative verb originally has an empty variable list, it would be of the excluded type \( \langle 0 \rangle \) if it were not identified with a quantifier contributed by an n-word. It is due to the fact that the \textsc{Neg Criterion} requires a quantifier of a type higher than \( \langle 0 \rangle \) on the verb’s \textsc{parts} list that identification with a quantifier from at least one n-word is necessary.

If we apply this reasoning to our example in \textbf{Figure 2} we see that the negative quantifier contributed by the n-word and the negative quantifier on the \textsc{parts} list

\(^{21}\) In formal notation:

\[
\forall \text{word} \; \varrho \text{. } \exists \text{excont} [\text{cat} \text{. } \text{head} \text{. } \text{cont} | \text{main} \text{. } \text{vform} \text{. } \text{fin}] \quad \land \quad \exists \text{no}(\vec{v}, \vec{a}, \beta) \land \varrho \land \vec{v} \neq () \land \varrho \triangleleft \beta
\]

\[
\rightarrow \exists \text{excont} [\text{sem} | \text{excont} \text{. } \text{excont} \text{. } \varrho] \quad \land \quad \exists \text{no}(\vec{a}, \vec{\gamma}, \delta) \land \vec{u} \neq () \land \exists \text{no}(\vec{u}, \vec{\gamma}, \delta) \land \vec{u} \neq () \land \exists \text{no}(\vec{u}, \vec{\gamma}, \delta) \land \vec{u} \neq () \land \exists \text{no}(\vec{u}, \vec{\gamma}, \delta) \land \vec{u} \neq ()
\]
of the verb must be identical. We obtain an obligatory NC reading, and the other two readings in (41) are correctly ruled out.

In sentences with more than one n-word such as (3c), the negative quantifier contributed by the verb must undergo resumption with at least one of the two quantifiers contributed by the n-words for the reasons just described. If one n-word does not undergo resumption with the NM and the other n-word, we obtain the DN reading in (43a). However, there is also the possibility that all the negative quantifier contributions in the sentence are identified. The number of variables contributed by the individual n-words determines the type of the resumptive quantifier. For (3c) with two n-words, each contributing one variable, the second available alternative is resumption of all three negative quantifiers, which leads to a quantifier of type $\langle 1^2, 2 \rangle$ for the NC reading, shown in (43b).

(43) a. $\text{no}(x, \text{student}'(x), \text{no}(y, \text{book}'(y), \text{read}'(x, y)))$ (DN)
b. $\text{no}((x, y), (\text{student}'(x), \text{book}'(y)), \text{read}'(x, y)))$ (NC)

Ionescu (2004) raises concerns regarding an analysis of nu as participating in resumption, because he believes that this would assimilate nu, as a contributor of a type $\langle 0 \rangle$ negative quantifier, to expletive negation in NC contexts. Expletive negation (abbreviated as $\text{nu}_{\text{expl}}$ below) is known to appear with some matrix verbs like a se teme ‘fear’ without contributing negative meaning. Since semantic negation does not arise in utterances with $\text{nu}_{\text{expl}}$, and since all lexical semantic contributions must be overtly visible in utterances according to one of the central principles of LRS, $\text{nu}_{\text{expl}}$ cannot possibly be associated with a type $\langle 0 \rangle$ negative quantifier. For that reason Ionescu’s apprehensions do not apply to the present proposal, where expletive negation does not contribute a type $\langle 0 \rangle$ negative quantifier. The assumption of semantic vacuity of expletive negation is supported by its inability to license strong NPIs like prea and by its inability to undergo resumption with negative quantifiers in (44a). By contrast, the NM nu always coincides with semantic negation. Consequently, it licenses strong NPIs and takes part in negative concord, as illustrated in (44b).

(44) a. $\text{Mă tem să } \text{nu}_{\text{expl}} \text{ (*prea}_NPI \text{) mă vadă vreunul/ *nimeni.}$
   me fear SJ not$_{expl}$ too$_{NPI}$ me see anyone/ *nobody
   ‘I fear that somebody might see me.’
b. $\text{Nu}_N \text{M (prea}_NPI \text{) mă vede nimeni.}$
   NM too$_{NPI}$ me sees nobody
   ‘Nobody can really see me.’

A description of the exact distribution of expletive negation requires a separate careful study, but we may note here that its occurrence is in complementary distribution with its NM function (see (45)). It can be accounted for by assuming that there is a lexical rule corresponding to the NM lexical rule in (38) that derives verbs marked by expletive negation, $\text{nu}_{\text{expl}}$. The input to this second rule is similar to the one for the NM lexical rule, but the output has the feature specification $[\text{nu expl}]$ and does not contain a negative quantifier in the word’s semantics.

(45) * $\text{Mă tem să } \text{nu}_{\text{expl}} \text{ nu}_N \text{M mă vadă Ion/nimeni.}$
   me fear SJ not$_{expl}$ not$_N$M me see John/*nobody
   (intended) ‘I fear that nobody will see me/John will not see me.’
4.3 Beyond Romanian core constructions

In this paper we focus on core constructions of negative concord in Romanian (finite verbs and their arguments) and their semantic description in terms of negative polyadic quantification. In the preceding sections we presented an analysis that covered simple clauses. In the present section, we outline how related constructions in Romanian fit into our approach, to be followed up by typological considerations in languages with different NC systems in Section 4.4.

We begin with a sketch of how we envisage the analysis of further Romanian NC constructions. These are (1) adverbial n-words, (2) fără ‘without’-NC constructions, (3) NC in non-finite clauses with the prefix ne- ‘non-’ on verbs, and (4) the combination of past participles with preverbal n-words.

Although we have left out adverbial NC constructions from our considerations above, it is well-known that adverbials participate in NC cross-linguistically (see (46) for Romanian). Our analysis predicts this behavior of adverbial negative quantifiers in case they are treated as (polyadic) generalized quantifiers, because NC is triggered by each configuration in which a negative quantifier of a type higher than (0) outscopes the verb. An analysis which follows the proposal for quantificational adverbs like always in de Swart (1993) and can be extended to also cover negative adverbs of manner (e.g., nici(de)cum ‘nohow’) and location (e.g., nicăieri ‘nowhere’) would thus be compatible with our Neg Criterion. How to spell out the analysis depends mostly on issues that are orthogonal to our present investigation, such as the exact choice of a tense semantics or an appropriate adaptation of a semantics of events. Once these are fixed, any lexical entry of an adverbial whose semantics comprises an underspecified negative quantifier automatically obeys the NC principles of Romanian.

(46) Ion nu a spus niciodată.  
John NM has said nothing never  
‘John never said anything.’

NC constructions involving fără ‘without’, as illustrated in (47), can be considered another hallmark of NC, as their counterparts are typically found in NC languages. In order to capture them, we have to extend the syntactic and semantic analysis to minor categories like the negative preposition at hand. In accordance with the standard treatment of prepositions in HPSG, let us assume that fără is the head of the phrase and may have either a verbal or a nominal complement. More specifically, the verbal complement is a subjunctive or non-finite verb phrase without a NM at the verb, i.e. [nu unmarked], or a nominal phrase.

(47) a. Ion a plecat fără (nu) spună/a (*nu) spune niciun cuvânt.  
John has left without SJ NM say/to NM say nothing  
‘John left without saying anything.’

b. Ion a plecat fără niciun cuvânt.  
John has left without no word  
‘John left without a word.’

The LRS analysis of the resulting prepositional phrases extends the Semantics Principle by a new clause that classifies these constructions as content raisers.
(Richter and Sailer (2004)), which raise the incont of the syntactic non-head to the head (the preposition). In addition, we assume that prepositions of the relevant type also raise the excont of the complement. The lexical semantics of fără suggests that it contributes an underspecified negative polyadic quantifier to the semantics, while its main predicate expresses a relation of accompaniment. Consequently, de Swart and Sag (2002) assume in their analysis that it is translated with a negative quantifier of type (0) that undergoes resumption with the negative quantifiers of its complements. In our architecture, fără requires identity of its negation with the negation of nominal complements that are negative quantifiers (47b). For non-finite verbal complements, fără is subject to the same constraint as finite verbs in Romanian are with the Neg Criterion. Due to the incont and excont identities at the syntax-semantics interface, an NC reading of (47a) is guaranteed.22

A third interesting area for NC are different types of non-finite constructions. The easiest case concerns NC in non-finite contexts in which the role of the NM is taken over by the prefix ne- ‘un-/non-’ as shown in (48).

(48) a. Nevenind/*Venind niciun student, ora s-a anulat. un.coming/coming no student, class the RF has canceled
   ‘Since no student came, the class got canceled.’

   b. Această carte necitată/*citată de nimeni trebuie să fie
      this book un.cited/cited by nobody must Sj be
      uninteresting
     ‘This book, which is not cited by anybody, must be uninteresting.’

The data in (48) can be captured by our analysis if we assume a variant of the NM Lexical Rule that is specialized for non-finite verb forms (with the exception of the infinitive). The output of the rule will essentially mirror the NM Lexical Rule for finite verbs in (38), except that the phonological function will have to be adjusted. With the lexical rule in place, we extend the applicability of the Neg Criterion in (42) to the new lexically negative non-finite verb forms. In effect this means that the licensing conditions of NC in those non-finite clauses are the same as for finite clauses.

This leaves an interesting residue of rather atypical cases of non-strict negative concord in Romanian. The preliminary exposition of Romanian data in Section 2 already showed an instance of a past participial construction in which a preverbal n-word contributes negation in the absence of a NM (see (6) and Ionescu (1999), for details). Teodorescu (2005) interprets these data in terms of a general contrast between NC in finite and non-finite constructions. According to her analysis, non-finite constructions involve a silent NM which is structurally situated above the

22 The lack of a negation prefix at the non-finite verb is presumably due to the presence of fără, which could be syntactically marked ([marking marked]), thus assimilating fără to HPSG’s marker category. One might argue that this lends additional support to the idea that Romanian n-words need a syntactic scope marker in verbal projections. As fără is a good scope marker in this context, no second scope marker is necessary. Its function as a scope marker is also a unifying property with negated finite verbs, which makes it plausible that the Neg Criterion applies to both, as the two elements serve the same syntactic purpose with respect to negation.
overt NM ne- and below the preverbal n-word, and licenses the latter. However, the data are not as uniform as this analysis suggests. In particular, present participles behave just as finite verbs with respect to preceding n-words. (49) shows that a non-finite construction with a preverbal n-word is ungrammatical in the absence of the NM ne- on the present participle verb.

(49) Nimeni *(ne)venind să deschiză ușa, au rămas pe-afară.
    nobody non-coming SJ unlock door-the, have remained outside
    ‘Since nobody came to open the door, they were left outside.’

With our interpretation of the data we follow the argumentation of Iordăchioaia (2004), who argues that the absence of a negation prefix in the presence of a preceding n-word in (6) is due to the adjectival nature of the relevant past participial constructions. This is confirmed by the fact that pre-adjectival n-words can also negate bona fide adjectives as in (50a). The present participle is usually verbal in Romanian, which explains the pattern in (49), although Teodorescu documents an instance of an adjectivized present participle, where the preposed n-word behaves just like in (6) (see (50b)).

(50) a. secretară nicio dată disponibilă
    secretary never available
    ‘a secretary who is never available’

b. mâncare deloc aburindă
    food at all steaming
    ‘food that is not steaming at all’

In conclusion, the contrast between past participles and finite verbs with preposed n-words correlates with a contrast between adjectives and verbs. A complete theory of NC outside the domain of finite verbs must be sensitive to this categorical distinction.

The distinction between adjectival and verbal NC contexts seems to be a peculiar property of Romanian; (Penka 2011, Ch. 2) shows that it is not present in strict NC languages such as Russian. In our account of Romanian, adjectival constructions differ from instances of NC in that the adjectival head is not subject to an NC constraint, which means that an n-word contributes its negation without triggering NC with a lexical head. This view of the matter is also supported by an observation of Ionescu (1999) and Teodorescu (2005), who report that in these constructions NC does not occur in combination with other n-words (see (51)).

(51) * articol de nimeni citat nicio dată
    article by nobody cited never

4.4 Remarks on the typology of negative concord

Any new analysis of NC has to be checked in light of how well it captures the varied landscape of NC across different languages. The present focus on putting forth,

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23 See Iordăchioaia (2004) for further properties of these constructions and an HPSG formalization in which negative quantifiers are treated along the lines of the Cooper storage mechanism of Pollard and Sag (1994).
and technically spelling out, polyadic negative quantification as the appropriate tool for an empirically adequate description of the NC facts of Romanian prohibits an in-depth discussion of typological data. In this section we briefly review the most salient properties of cross-linguistic variation in Romanian, Polish, French, Italian and German in order to indicate which parts of our theory will serve as pivot for variation, and which features of the analysis remain fixed.

The first formulation of a Neg Criterion in HPSG was presented by (Richter and Sailer 2004, p. 125) in an LRS analysis of NC in Polish. This analysis was based on an interpretation of n-words as (negative) monadic quantifiers and used the idea of identifying negative quantifiers originating from different lexical contributors at the syntax-semantics interface. The authors deliberately called their central principle of Polish Neg Criterion after a constraint that Haegeman and Zanuttini (1991) had formulated much earlier in a different grammar framework, because the function of the HPSG principle was designed to express similar insights into the mechanisms behind NC. In Haegeman and Zanuttini’s formulation the Neg Criterion essentially requires that n-words and sentential negation enter a Spec-Head relation; variation between languages is a consequence of whether the rule applies at S-structure or at LF in combination with further conditions on n-words and sentential negation in a particular language.

Still following the spirit of the proposal by Haegeman and Zanuttini in disguise of its translation into HPSG and LRS by Richter and Sailer, we take n-words and (non-expletive) sentential negation to express semantic negation across languages. We model linguistic variation by the interaction of language specific variants of the Neg Criterion with lexical variation of key lexical elements in the negation systems of the respective languages. This means that the syntactic (or morphological) nature of the negation particle or negation adverb or negation argument or negation suffix of a verb may vary, and single words participating in negation contexts or entire classes of (n-)words may carry additional restrictions that might have to do with the overall linguistic system in which they are embedded. Although this interaction can result in initially quite puzzling data configurations, the underlying categorial theory is rather simple: We adopt the typological theory of NC in Polish, French and German of Richter and Sailer (2006), adding Romanian and Italian, and generalizing the interpretation of sentential negation and n-words from classical negation and monadic negative quantifiers to n-ary polyadic quantification. It follows that the different NC systems in the five languages under consideration must be due to variation in (a), the Neg Criterion, and (b), additional constraints that can be lexical or syntactic in nature.

For Polish, French and German, we adapt Richter and Sailer’s account to negative polyadic quantification. Restricting our attention to simple finite clauses, Polish and (standard) German mark the two ends of the NC continuum: Polish is a strict NC language in which no double negation readings are possible, and Ger-

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25 For example, negative polar indefinites are in distributional competition with n-words in strict NC languages and in weaker competition in non-strict NC languages, with non-NC languages providing yet another set of restrictions on the distribution of both types of elements, n-words and corresponding negative polarity items. See Hoeksema (2010, 2012) for thrilling cross-linguistic observations on different kinds of contextual effects on the diachronic development of fine-grained lexical distribution patterns in connection with negation.

26 See Richter and Sailer (2006) for a comprehensive discussion of data for all three languages, which we do not replicate here. The French data are all from European French. Especially with respect to the NC behavior of pas ‘not’, European French differs from other varieties of French.
man is a non-NC language. The occurrence of an n-word in a Polish finite clause necessitates the presence of the verbal negation prefix \textit{nie}, and the interpretation is always NC, independent of the number of n-words (52a). In German, the sentential negation adverb \textit{nicht} ‘not’ and any n-word in a clause require the independent realization of their negative semantic contribution to the clause (52b). In addition, German does not require a sentential adverb in order to express sentential negation (52c).

\begin{enumerate}
\item \textbf{Nikt} *(nie) rozmawiał z \textbf{nikim}.
\textit{nobody not talked with nobody}
\textit{‘Nobody talked with anybody.’}
\item \textbf{Niemand} ist \textit{nicht} gekommen.
\textit{nobody is not come}
\textit{‘Nobody did not come.’}
\item \textbf{Niemand} ist gekommen.
\textit{nobody is come}
\textit{‘Nobody came.’}
\end{enumerate}

The Polish \textbf{Neg Criterion} is stricter than the Romanian \textbf{Neg Criterion}: Whenever a negative quantifier of type higher than type \langle 0 \rangle outscopes a finite verb in its \textit{excont}, its variable must be in the variable vector of a negation on the \textit{parts} list of the verb. Verbs with negation prefix are formed with a \textbf{NM Lexical Rule} like in Romanian. The strengthened \textbf{Neg Criterion} for Polish enforces the negation prefix on the verb in the presence of an n-word, and it guarantees that each n-word enters NC. While the \textbf{Neg Criterion} for Polish does not permit DN readings at all, its Romanian counterpart only excludes DN triggered by the negative marker, a negative quantifier of type \langle 0 \rangle.

In German NC is impossible: According to the analysis of Richter and Sailer (2006), the German \textbf{Neg Criterion} takes the form of a \textbf{Negation Faithfulness Constraint}, which requires that each negation be expressed independently. This amounts to saying that each lexically introduced negation must be uniquely visible in the interpretation of a clause. If there are two negations, no matter whether they come from two n-words or an n-word and the sentential negation adverbial, they will be perceived as double negation.\textsuperscript{27} Moreover, the occurrence of an n-word is not contingent on the occurrence of the negation adverbial.

French occupies an intermediate position, with n-words generally permitting but not enforcing NC. At the same time, the lexeme for sentential negation, \textit{pas} ‘not’, exhibits lexically idiosyncratic distributional behavior.\textsuperscript{28} We follow Rowlett (1998) in assuming that the preverbal particle \textit{ne} is an expletive that does not express negation in European French.

First of all, we observe that an n-word (\textit{personne ‘nobody’}) is sufficient to express sentential negation (53a).\textsuperscript{29} However, if there are two n-words as in (53b),

\textsuperscript{27} Negation faithfulness only applies to standard German. There is a certain amount of dialectal variation with respect to the availability of NC.

\textsuperscript{28} Richter and Sailer (2006) discuss the diachronic reasons for the peculiar distribution properties of \textit{pas} and relate them to dialectal synchronic data that suggests an analysis in terms of lexical distribution restrictions. HPSG supports a precise formulation of these constraints.

\textsuperscript{29} All French examples are from Richter and Sailer (2006).
there is a contextually determined choice between an NC reading and a double negation reading. The examples in (53c) and (53d) show that this choice is not available with *pas*: A preverbal subject n-word and a postverbal object n-word both lead to a double negation reading.

(53)  
   a. Jean n’a parlé à personne.
       Jean NE has talked to nobody
       ‘Jean hasn’t talked to anyone.’
   b. Personne n’a rien dit.
       nobody NE has nothing said
       ‘Nobody said anything/nothing.’
   c. Personne n’est pas venu.
       nobody NE is not come
       ‘Nobody did not come.’
   d. Jean n’a pas parlé à personne.
       Jean NE has not talked to nobody
       ‘Jean did not talk to nobody.’

The French NC system will be obtained by a liberal Neg Criterion which leaves the occurrence of negation identities unregulated. Negative polyadic quantifiers contributed by n-words that outscope the finite verb may either scope independently (double negation readings) or enter into a joint n-ary negative polyadic quantifier (NC readings). Without anything else being said, any combination of this is possible for more than two n-words, although we expect that information structural restrictions and restrictions on scope will play an important role in determining the actual interpretation possibilities. The negative adverb *pas* is a lexical exception from this liberal behavior. According to Richter and Sailer, it has a lexical collocation restriction reminiscent of the German Negation Faithfulness Constraint to the effect that the negation contributed by *pas* may not enter into NC with other negative quantifiers.

Let us finally consider finite clauses in Italian, another non-strict NC language that behaves different from both Romanian and French, and serves well to illustrate the effect of more subtle variants of the Neg Criterion and its interaction with the NM Lexical Rule. The initial two examples suggest a familiar picture: A NM contributes sentential negation alone (54a), and a postverbal n-word requires the presence of the NM on the verb (54b), leading to a single negation reading.

(54)  
   a. Gianni non ha telefonato a sua madre.
       John NM has phoned to his mother
       ‘John didn’t call his mother.’ (Zanuttini (1994))
   b. *(Non) ho visto nessuno.
       NM have seen nobody
       ‘I haven’t seen anybody.’ (Zanuttini (1994))

However, the next set of data deviates from the Romanian pattern we saw earlier. A preverbal n-word contributes negation alone and licenses NC with other postverbal n-words (55a). The special status of a preverbal n-word is further confirmed by its interaction with the NM on the verb, and with other postverbal
n-words. A preverbal n-word co-occurring with a NM can only be interpreted as DN (55b), and adding another postverbal n-word does not change the DN reading (55c).30

(55)  

a. **Nessuno**/*Gianni ha detto niente.**
nobody/Gianni has said nothing

‘Nobody/Gianni said anything.’ (Zanuttini (1994))

b. **Nessuno non** vede questo cartello.
nobody NM sees this sign

‘Nobody does not see this sign.’ (DN) (Corblin and Tovena (2001))

c. **Nessuno non** porta un fiore a nessuno.
nobody NM brings a flower to nobody

‘Nobody does not bring a flower to anybody.’ (DN) (Corblin and Tovena (2001))

In order to capture this pattern in our present NC architecture, we need to extend the notion of negation marking at the verb. Evidently, it is not only the preverbal NM that plays this role in Italian, a preverbal n-word can do so as well. The first step to express this in the grammar would be a modification of the NM Lexical Rule on verbs. Its Italian counterpart distinguishes two cases. In the first one, which is similar to Romanian, a negation prefix is attached to the verb, but this time with the additional restriction that the subject’s variable may not be included in the variable vector of the polyadic negative quantifier. This excludes NC with the subject in sentences (55b) and (55c), while it provides the observed interpretation of (54a) and (54b). The second possibility for the rule output is a verb without NM prefix that introduces a negative polyadic quantifier which contains the subject variable on its variable vector. This is the situation in which a negative subject licenses the morphologically invisible negation on the verb. It is realized in simple negation readings with an n-word as subject and in NC constructions like (55a).

Since Italian subjects can act as negation markers, the Italian Neg Criterion has to take note of them. Its condition on Italian finite verbs says that if a non-subject negative quantifier outscopes the finite verb in the verb’s excont, then the non-subject’s variable must be on the variable vector of the verb’s negative quantifier. In other words, non-subject n-words are in NC with negated verbs. In combination with the NM Lexical Rule, this makes the NM or a subject n-word obligatory in (54b) and (55a). The interaction of the NM Lexical Rule and the Neg Criterion also determines that a preverbal n-word in combination with a morphological NM on the verb entails a double negation reading ((55b)–(55c)), as their negative semantics must be independent.

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30 For this quick overview of Italian core data, we ignore left dislocation, which we assume to be correlated with additional information-structural effects. We should also note that DN readings in Italian are reportedly highly marked and very context-dependent.
5 N-words in embedded subjunctive clauses

To complete our analysis of Romanian, we investigate the function of the NM in NC constructions and show that our theory can be extended to account for locality conditions on the scope of negative quantifiers in NC constructions in complex sentences.

5.1 The NM as a scope marker

We argued that the NM cannot be a semantic licenser of n-words, as it does not maintain anti-additivity in the relevant contexts (12). We also saw that in NC constructions the negation contributed by the NM must always undergo resumption with at least one n-word, as decreed by the Neg Criterion for Romanian (42). But if the NM is neither a semantic licenser, nor a real negation contributor in NC, what is its role in these constructions and why is it obligatory with n-words?

We think that an answer to these questions can be found in complex sentences like (56) where an n-word is contained in an argument phrase in an embedded subjunctive clause. In this kind of construction the negative quantifier may take wide scope over the matrix verb (56a) or narrow scope within the subjunctive clause (56b). Parallel observations hold for English n-words embedded in infinitival clauses (57). But unlike in the ambiguous English construction, in Romanian the scope of the quantifier is resolved by the (obligatory) NM: The scope of the negative quantifier is associated with the verb that carries the NM ((56a) vs. (56b)). We see that the NM functions as a syntactic licenser for n-words; the NM marks the sentential scope of the negative quantifier (cf. also Ionescu (1999, 2004)).

(56) a. Ion nu i-a cerut Mariei [să citească nicio carte].
   John NM CL-has asked Mary [sJ read no book]
   ‘There is no book that John asked Mary to read.’

b. Ion i-a cerut Mariei [să nu citească nicio carte].
   John CL-has asked Mary [sJ NM read no book]
   ‘John asked Mary not to read any book.’

(57) I will force you to marry no one. (Klima 1964, p. 285)

a. ‘I won’t force you to marry anyone.’

b. ‘I would force you not to marry anyone.’

Assume that we modify the lexical semantic specifications of Section 4 by adding world arguments of type s to the non-logical constants for predicates and noun phrases in the usual way, i.e. we will now use the full type theory of Ty2 in our specifications. Moreover, assume for the moment that the excont of matrix and embedded clause are distinct. With these modifications and assumptions, which we will explain in more detail in Section 5.2, our theory captures (56a) and (56b).

31 Like English and other languages, Romanian also has Neg raising verbs, which we do not discuss here, but would be covered by the analysis in Sailer (2006), which is fully compatible with our present account of negative concord.

32 We will assume that proper names are rigid designators.
In both sentences, independent LRS principles for quantifiers in argument position dictate that the negative quantifier associated with *nicio carte* must outscope the verb in the embedded clause. Let us look at (56a). Suppose *nicio carte* takes scope in the embedded clause. Then the Neg Criterion is violated since the non-negated verb cannot have a negative quantifier on its parts list. Suppose it takes scope in the matrix clause. Then the Neg Criterion is satisfied by resumption of the negative quantifier from *nicio carte* with the quantifier of the negated verb. We obtain the truth conditions: no\((y, \text{book}^x_w(y), \text{ask}^x_w(\text{john}',\text{mary}',\lambda w.\text{read}^x_w(\text{mary}',y)))\).

The converse holds in (56b). The embedded verb has a negative marker and a negative quantifier on its parts, which means that *nicio carte* can take scope within the verb’s excont by resumption \(\text{ask}^x_w(\text{john}',\text{mary}',\lambda w.\text{no}(y, \text{book}^x_w(y), \text{read}^x_w(\text{mary}',y)))\). It cannot take scope in the matrix clause, because the matrix verb lacks a negative quantifier on its parts list.

5.2 An intensional fragment of Romanian

In order to formulate truth conditions for sentences that are embedded under propositional attitude predicates, we add appropriate possible world arguments to our non-logical constants and modify the lexical entries of finite verbs: As can be seen in (58) below, verbs now contribute a world variable and lambda abstraction over that world variable, where the lambda abstraction is lexically constrained to take place in the external content of the verb.

For simplicity, we adopt the standard textbook analysis of propositional attitude verbs and finite sentences of (Gamut 1991, Chapter 6), which closely follows the design of Montague’s PTQ fragment. The only substantial new technique in our Romanian grammar fragment compared to Section 4 concerns the treatment of embedded sentences as propositions and the way we ensure that root clauses still denote truth values in spite of the fact that every finite verb has a lambda abstraction over its contributed world variable. In effect, finite verbs introduce restrictions on the distribution of world variables which, as a consequence of routinely applying the combinatoric semantic principles of LRS, will force matrix clauses to be of logical type \(t\), while embedded sentences are analyzed as propositions. Propositions denote sets of worlds and are of type \(\langle s, t \rangle\). We assume that a grammar principle demands that unembedded signs (in our fragment: declarative sentences) be of type \(t\), and their external content has the form \((\lambda w.\phi)(w)\).\(^{33}\) Apart from the types of (most) non-logical constants, nothing else will change in our grammar fragment, not even the representations for polyadic quantifiers and their types.

To illustrate and explain the changes, we extend the specification of the negative verb form *nu a venit* from Section 4. The reader might recall that it describes a verb form that is licensed in the grammar as the output of the NM Lexical Rule.

\(^{33}\) Unembedded signs in HPSG are the type of signs which occur as independent utterances; they also play a crucial role in the model theory of grammars. See Richter (2007) for details. An extension of our present fragment would of course allow other unembedded signs beyond declarative sentences.
The logical constant *come*' (see the main value) is now of type \(<s,⟨e,t⟩⟩\). We notate the additional argument, a world variable, as a subscript (as shown in the incont) to distinguish it clearly from the argument of type *e*, which will typically be a constant in our example sentences below. The parts list reveals that finite verbs now introduce a lambda abstraction with respect to a world variable \(w\) over a sentence \(⟨w⟩\), and they contribute the world variable themselves to the semantic specification (second element of the parts list). In additional restrictions we require that the lambda abstraction be inside the external content of the verb, the negation be in the scope of the lambda abstraction, and the constant *come*' be in the restrictor of the negation (the latter as before). The last restriction in (58) says that the world variable, \(w\), is the argument of a proposition, \(φ'\). In a simple clause, this restriction will ensure that the semantic type of the truth conditions is a logical sentence. This is the type of expression that an HPSG grammar with semantic specifications in Ty2 requires of the logical specification of unembedded utterances. For embedded clauses, the constraint \(φ'(s,t)(w)\) will not be satisfied by the embedded proposition; it will be satisfied at the level of the matrix clause.

With these adjustments in place, we can explain the form of the new excont values of finite sentences.

\[
(59) \quad \text{Ion nu a venit.} \\
\text{John NM has come} \\
a. \quad (λ_w. \text{no}((),(),\text{come}'_w(\text{john}')))(s,t)(w) \\
b. \quad \text{no}((),(),\text{come}'_{s_0}(\text{john'}))
\]

The familiar example *Ion nu a venit* (‘John didn’t come’) receives the excont value shown in (59a). We will simplify this type of logical expressions to formulas such as the one shown in (59a), which results from beta-converting (59a) and following the linguistic naming convention of designating the world in which an expression is evaluated with the first variable of type *s*, *s_0*.

The interaction of the lexical restrictions on the truth conditions on finite verbs with other semantic composition principles is hardly more intricate in complex sentences with propositional attitude verbs as matrix predicates. In this section, we are ignoring the interaction with other grammar principles, and restrict attention to the distribution of the newly introduced lambda abstraction and world variable.
For the sentence in (56b), in which the negative quantifier contributed by the nominal phrase *nicio carte* scopes in the embedded clause, we obtain the truth conditions in (60a) as EXCONST value.

(60) Ion i-a cerut Mariei [să nu citească *nicio carte*].

a. \( \lambda w.\text{ask}_w'(\text{john}', \text{mary}', \lambda w.\text{no}(y, \text{book}_w'(y), \text{read}_w'(\text{mary}', y))) (w) \)

b. \( \text{ask}_w'(\text{john}', \text{mary}', \lambda w.\text{no}(y, \text{book}_w'(y), \text{read}_w'(\text{mary}', y))) \)

The argument of *ask*’ that contains the truth conditions of the sentential complement is a proposition (type \( ⟨s, t⟩ \)), as required by the typing of the constant *ask*’, \( ⟨s, ⟨⟨s, t⟩⟩, ⟨e, ⟨e, t⟩⟩⟩⟩ \). The world variable \( w \) that originates from the predicate *să nu citească* in the embedded clause thus cannot be realized as an argument of the proposition in the third argument slot of *ask*’, as this would lead to a type mismatch. The constraint \( φ'_{⟨s, t⟩}(w) \), which is introduced twice, once by the matrix verb and once by the embedded verb, can only be satisfied by applying the representation of the proposition constructed in the matrix clause to \( w \). Note that each finite verb introduces the same world variable. This will lead to the correct result, as each occurrence of \( w \) is bound by a particular lambda operator.

(60b) repeats the notational conventions for EXCONST values of root clauses which we already introduced for the simple clause in (59), and which we will use for readability in the following discussion: By beta-conversion and naming the world variable of the matrix clause \( s_0 \), we arrive at a simpler form of the actual EXCONST value (60a), which is the form of the expression as it is actually specified in the grammar principles.

5.3 Complex sentences with two NMs

The situation becomes more complex—and also more interesting—when both the matrix and the embedded verb in a complex clause carry a NM:

(61) Ion *nu* i-a cerut Mariei [să *nu* citească *nicio carte*].

John NM CL-has asked Mary SJ NM read no book

a. ‘There is no book John asked Mary not to read.’

b. ‘John didn’t ask Mary not to read any book.’

The sentence (61) has two readings as indicated in the two translations. The negative quantifier *nicio carte* may enter NC with the matrix verb (61a) or with the embedded verb (61b). In either case, the other verb contributes a type \( ⟨0⟩ \) negative quantifier to the interpretation. This means that one negation outscopes the other.

In preparation of our analysis of (61), we start our discussion with the simpler case of a complex sentence without n-words but with a NM at the matrix verb and the embedded verb (62). The relevant parts of its analysis tree are shown in Figure 3.

(62) Ion *nu* i-a cerut Mariei [să *nu* citească *Nostalgia*].

John NM CL-has asked Mary SJ NM read the nostalgia.book

‘John didn’t ask Mary not to read *The Nostalgia*.’
The excont of the non-head daughter VP on the right, which is the embedded subjunctive clause, must be an element of the parts list of that VP (Excont Principle). Let us first consider the options for this excont value from the perspective of the embedded clause alone, ignoring possible requirements of its matrix environment. The smallest piece of semantic representation which is eligible without violating any other LRS principles is the incont value $3$. The largest piece of semantic representation that the excont $0$ of the embedded subjunctive clause can be identified with is the lambda term $\lambda w.\psi$. A third option seems to be the negative quantifier $11$, which is contributed by the verb să nu citească and is licensed by the NM Lexical Rule. However, since the output of the lexical rule guarantees that this negative quantifier is a subterm of the scope of the lambda abstraction which in turn is a subterm of the external content of the verb, we are forced to conclude that $0$ equals $9$, the largest possible candidate for the excont value, which we already considered before.

Next, we have to consider the matrix environment of the embedded VP. It may be surprising that the conditions discussed so far do not prevent the negative quantifier of the embedded verb in Figure 3 from taking scope in the matrix sentence. The reason is that nothing forces the quantifier $11$ to take immediate scope over the predicate $3$. Other functors or operators can intervene. As a consequence, $11$ may be identified with the matrix negation or trigger DN within the matrix clause. Neither of the resulting semantic representations expresses possible truth
conditions for the sentence in (62). If our reasoning so far were complete, a NM at an embedded verb could even outscope an affirmative matrix verb, giving the sentence in (63) the reading in (63b).

(63) Ion i-a cerut Mariei [să mi citească Nostalgia].
      John CL- has asked Mary SJ NM read nostalgia.the
      a. ‘John asked Mary not to read The Nostalgia.’
      b. # ‘John didn’t ask Mary to read The Nostalgia.’

However, we also have to take the typing restrictions of the matrix predicate into account. They require that the sentential argument be represented by an expression of type \( \langle s, t \rangle \). This can only be the case if the lambda abstraction originating with the verb in the complement clause is realized in the argument slot of the matrix predicate. Since the negation of the embedded verb is constrained to be in the scope of the lambda abstraction, it can not take scope outside of the embedded clause.

Moreover, we independently want to restrict the external content of embedded sentences more tightly in order to confine scope projection conditions of finite verbs to their syntactic projection. To this end, a new clause of the SEMANTICS PRINCIPLE ensures that the external content of the complement clause of a propositional attitude verb remains within the scope of the matrix verb:

(64) **The Semantics Principle, Clause 3**
      If the head-daughter of a phrase has a main value with a propositional argument \( \eta \) and the non-head-daughter is a propositional complement, then the excont value of the complement must be a subterm of \( \eta \).

In our example in Figure 3 the new clause of the SEMANTICS PRINCIPLE makes the excont of the subjunctive clause a subterm of the scope \( \eta \) of the verb \( \text{ask}' \). The negative quantifier contributed by the NM on the embedded verb is a subterm of the lambda abstraction which in turn is a subterm of \( \eta \). The only reading we obtain for (62) is the one in which both verbs are negated (65), as desired.

(65) \( \text{no}() , () , \text{ask}'(\text{john}' , \text{mary}' , \lambda w.\text{no}() , () , \text{read}'(\text{mary}' , \text{nostalgia}')))) \)

Everything is now in place for the analysis of the two readings of the ambiguous sentence (61). A description of the tree structure is given in Figure 4. The only difference from Figure 3 is the negative quantifier in the embedded VP which takes the position of the proper name Nostalgia. For reasons of space, information carried by identical tags as in Figure 3 is not repeated in Figure 4.

There are three negative quantifiers whose scope interaction must be determined. The restriction \( [i] \in [\eta] \) (known from the previous example) and the identity of \( \eta \) with the exc of the embedded clause \( \eta = [\eta] \) leave two possibilities: the scope \( \psi \) of the lambda abstraction \( \lambda w.\psi \) could be identical with \([i]\) or with \([ii]\). If \( \psi = [i] \) we are in the situation in which the negative quantifier \([ii]\) of \text{nimic carte} is interpreted in the embedded clause: Being identical with \( \psi \) it is a subterm of \( \eta \) and cannot take scope in the matrix clause. On top of this, the NEG CRITERION forces resumption between \([i]\) and \([ii]\). We obtain a NC reading in the subjunctive clause and the interpretation (66a) for (61). If we start with the possibility of \( \psi = [ii] \)
without making initial commitments about the nature of the negative quantifier could also take scope in the matrix clause where it would then undergo resumption with to satisfy the Neg Criterion. The result is a NC reading in the matrix clause and the interpretation (66b) for (61):

\begin{align*}
\text{(66)} \quad & \text{a. } \text{no}()(), \text{ask}_w^{10}(\text{john}', \text{mary}', \lambda w. \text{no}(y, \text{book}_w^{10}(y), \text{read}_w^{10}(\text{mary}', y))) \\
& \text{b. } \text{no}(y, \text{book}_w^{10}(y), \text{ask}_w^{10}(\text{john}', \text{mary}', \lambda w. \text{no}(), (), \text{read}_w^{10}(\text{mary}', y)))
\end{align*}

In this section we showed that our theory of NC in Romanian contains all the ingredients required to account for the properties of negative quantifiers and NC in complex clauses, and we integrated our theory of polyadic quantifiers with two-sorted type theory. The analysis is still incomplete in at least one important respect: We did not carefully consider the full range of data that is relevant for a comprehensive theory of NC in complex sentences. The empirical questions are quite challenging. What interpretations are available for negative quantifiers in complex sentences with two or more n-words? An unconstrained theory predicts scope interactions that native speakers most likely will not perceive given the usual difficulties with multiple negations. It will be important for future extensions of our theory to find out which readings are available and preferred, and which grammatical or processing constraints are at play. We expect that only carefully controlled experimental studies can provide reliable answers to these empirical issues.
6 Conclusion and further issues

The present analysis of NC in Romanian elaborates the approach that was pioneered by an analysis of French in de Swart and Sag (2002). Our theory considerably extends de Swart and Sag’s proposal by explicitly integrating a higher-order logic with polyadic quantification in HPSG and making all semantic composition principles for polyadic quantification entirely explicit. We believe that the formulation of the polyadic quantifier approach to NC in LRS is fully compatible and can in fact subsume the typological theory of NC in Polish, French and German presented in Richter and Sailer (2006), even though that theory was formulated on the basis of monadic quantification. To the extent that we were able to explore the compatibility of our analysis with their much broader typological considerations (Section 4.4), we do not see any obstacles to express obligatory NC in Polish, optional NC in French, and absence of NC in German in terms of restrictions on possible resumption of negative quantifiers. Future work should still spell out the necessary semantic composition constraints with more formal rigor and in a more systematic way, testing out the robustness and plausibility of the general framework in capturing fine-grained typological variation by gradually varying constraints on semantic composition and their interaction with the idiosyncratic behavior of lexical items that play a prominent role in the negation systems of different languages. For these future developments we would like to attach particular interest to the behavior of languages like Italian, which require additional refinements of the NC conditions concerning preverbal n-constituents.

With negative concord we addressed a rather special case of applying the tool of polyadic quantification to the analysis of a family of data in natural languages: The negative polyadic quantifiers we defined are decomposable into iterations of monadic quantifiers. To argue for our analysis, we had to show that it involved the most parsimonious set of assumptions which could describe the full range of data of Romanian NC and could do justice to the observable meaning of n-words and the verbal negation prefix in isolation as well as in various syntactic constellations. We were not in a position to argue that polyadic quantifiers are an absolute technical necessity to derive the readings of the Romanian sentences that we investigated. The fact that their description is in principle possible under traditional assumptions about semantic compositionality with a higher-order logical language based on a functional theory of types is perhaps the main reason why researchers have been hesitant to step outside these well-established boundaries to obtain what we consider a much simpler picture of the landscape of negative concord. Recall that we did not appeal to the usual host of unobservable empty categories that easily complicate assumptions about syntactic structure (let alone the machinery required for efficiently parsing these structures), and we did not introduce at least equally problematic but analytically essential empty semantic operators that are only justified by complex nonlocal syntactic licensing conditions whose exact inner workings are rarely pursued to full formal explicitness.

The real potential of a fully explicit integration of polyadic quantification with precise syntactic and semantic assumptions only comes alive when we turn to expressions whose interpretation is no longer amenable to the decomposition of polyadic quantifiers into monadic quantifiers. These are cases of so-called irreducible polyadic quantifiers, which we already referred to in passing and for comparison with NC in Section 2.4: Our examples there included cumulative quantifiers...
and readings obtained with same/different (25). If one accepts that these constructions are genuine cases of quantification and that the assumed readings correctly reflect their semantics (rather than being a consequence of additional repairs at some post-semantic or pragmatic level), one is also forced to tell a story about their integration in a mathematically exact grammar framework. Adding polyadic quantification to LRS answers to this need and opens the door to exploring a whole range of new semantic phenomena that have not been explored in model-theoretic grammar frameworks like HPSG, including the afore-mentioned cumulative and same/different (unreducible) polyadic quantifiers, and other similar constructions well-known in the semantic literature on quantification (Keenan (1992), Keenan and Westerståhl (1997)). Since the present constraint-based syntax-semantics interface supports polyadic quantifiers, HPSG theories can start to investigate them in the context of concrete syntactic analyses. This brings within reach a hitherto impossible explicit specification of the syntax and semantics of constructions that require unreducible polyadic quantifiers for an adequate rendering of their truth conditions and have, for that reason, eluded a comprehensive treatment in other grammar frameworks.

Acknowledgments: We would like to thank five anonymous reviewers and our NLLT editor, Louise McNally, for insightful criticism and numerous suggestions for improvements. It is only due to their persistent requests that the presentation of LRS became as self-contained as it is. Students at Universität Tübingen and the audience of the 2009 International HPSG Conference in Göttingen asked for clarifications that informed subsequent modifications. Christopher Piñón and Ivan Sag went to great lengths to provide extensive comments that led to substantive revisions and what we hope is a much more lucid line of argumentation than in earlier drafts. Janina Radó did the proofreading, bringing our thoughts into readable shape. Without Manfred Sailer we would not have written this paper. Barbara Partee has much more to do with it than meets the eye: Thank you!

References


34 A symptomatic example for the conceptually unsatisfactory situation in the framework of compositional LF-semantics is provided by the analysis of exception sentences in (Moltmann 1995, p. 275–276). As the desired integration of polyadic quantification is impossible, the theory must be formulated on a post-semantic level of implications which need to repair the semantics. Major architectural design decisions should not be forced upon linguists by limitations of their framework but rather by empirical evidence.


